

*Bridging Length-Time Scales in a Brittle-Ductile Process :
evolution of “defects” in fast-slow time space*

H.O’Ghaffari

In collaboration with :

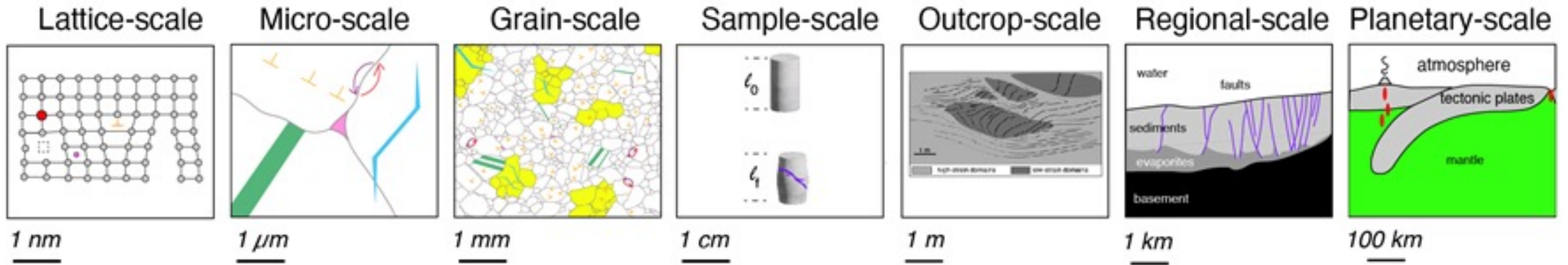
T.Mittal, B.Evans, B.Holtzman & M.Pec



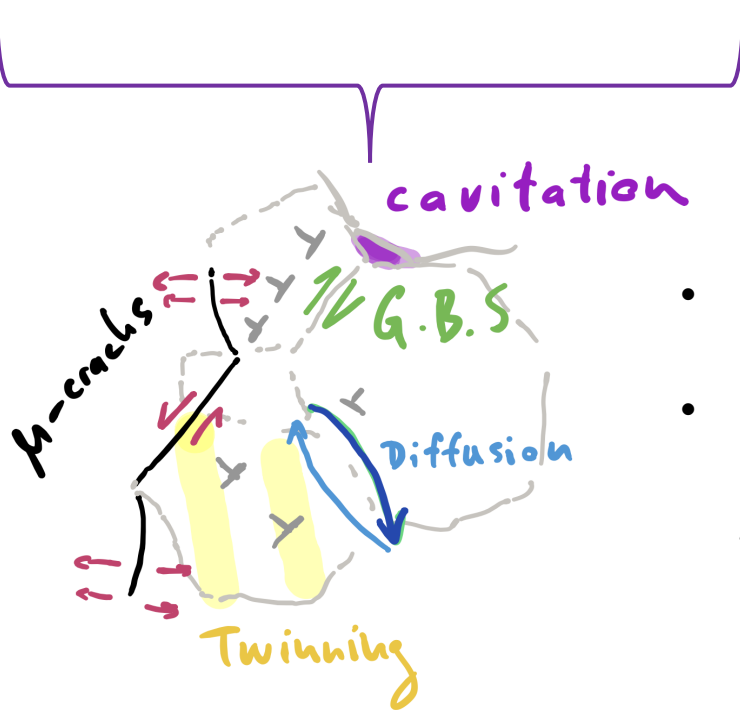
Massachusetts Institute of Technology, Dept. of Earth, Atmospheric & Planetary Sciences



- Length scales which control deformation processes in geomaterials...

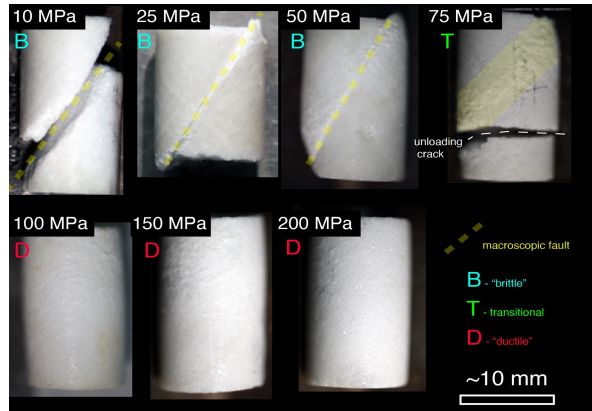


O'Ghaffari, Mittal & Pec, in progress, 2023

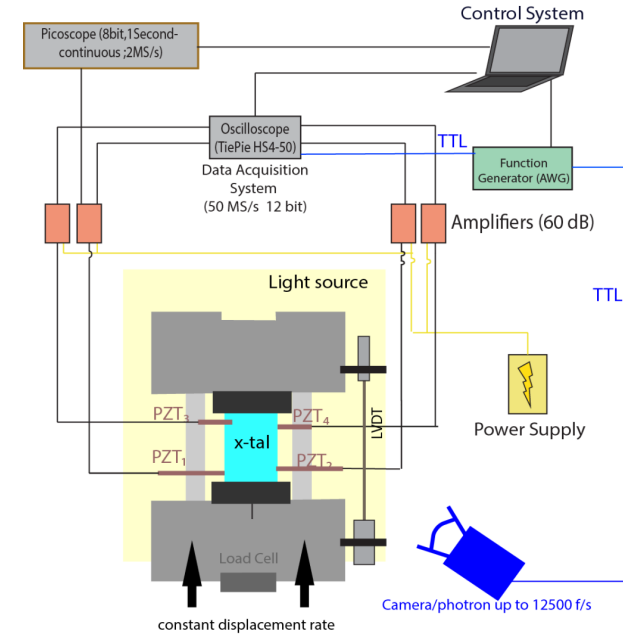
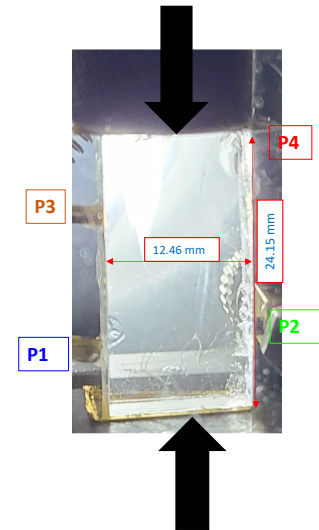
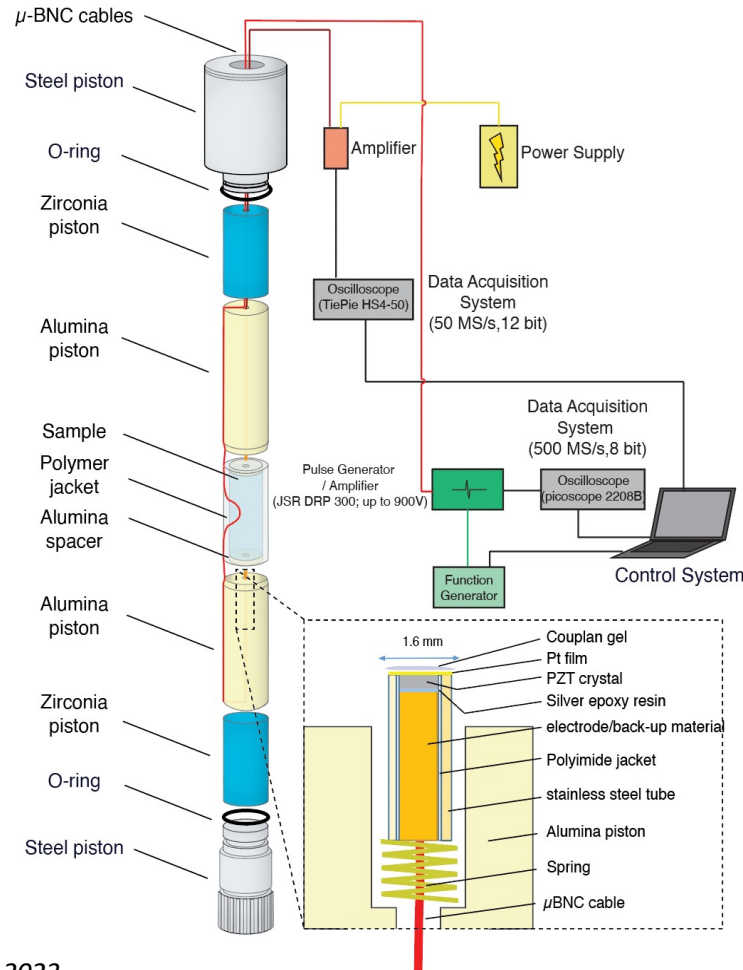


- Rise and freeze-out of defects
- Interactions of defects gives rise to complexity of deformation modes [brittle/Ductile//semi-brittle...]: **Probing Deformation phase in micro/macro-scales**

Marble Samples & Calcite Single Crystal : Active & Passive in fast-slow time space

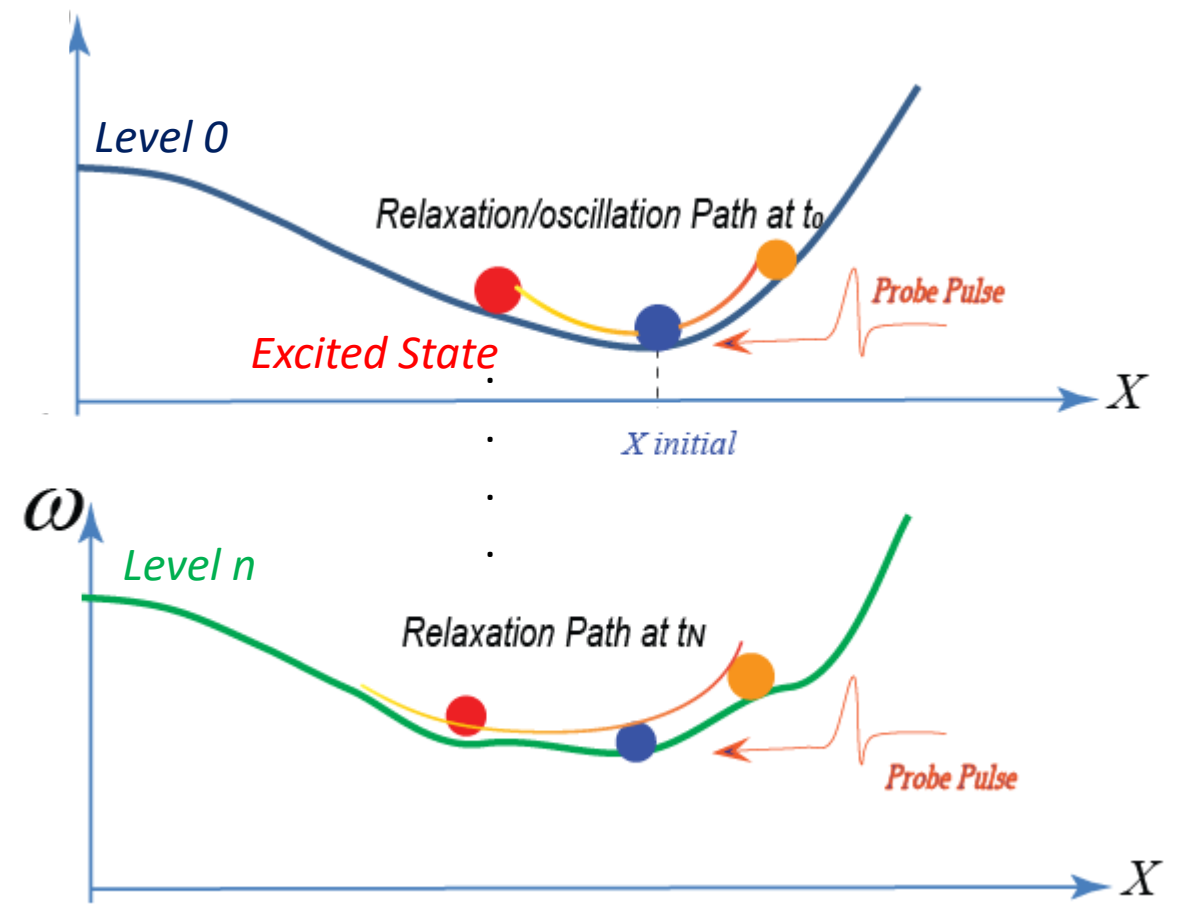
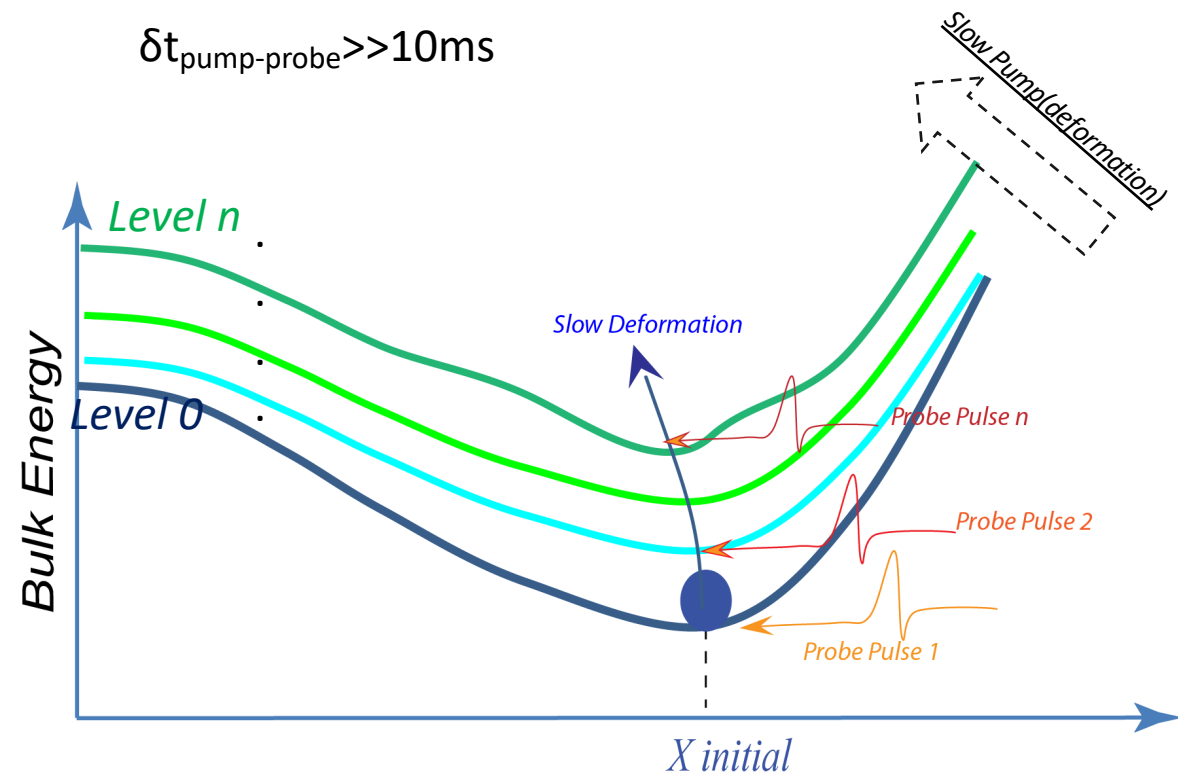


Marble Samples



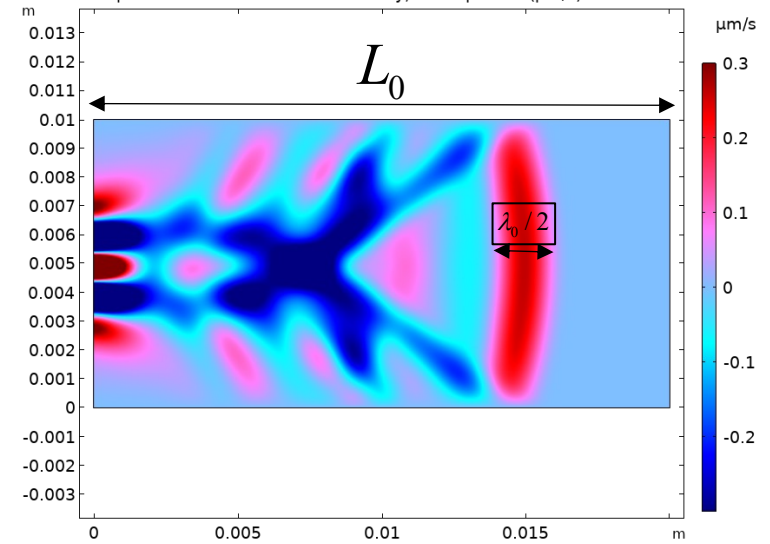
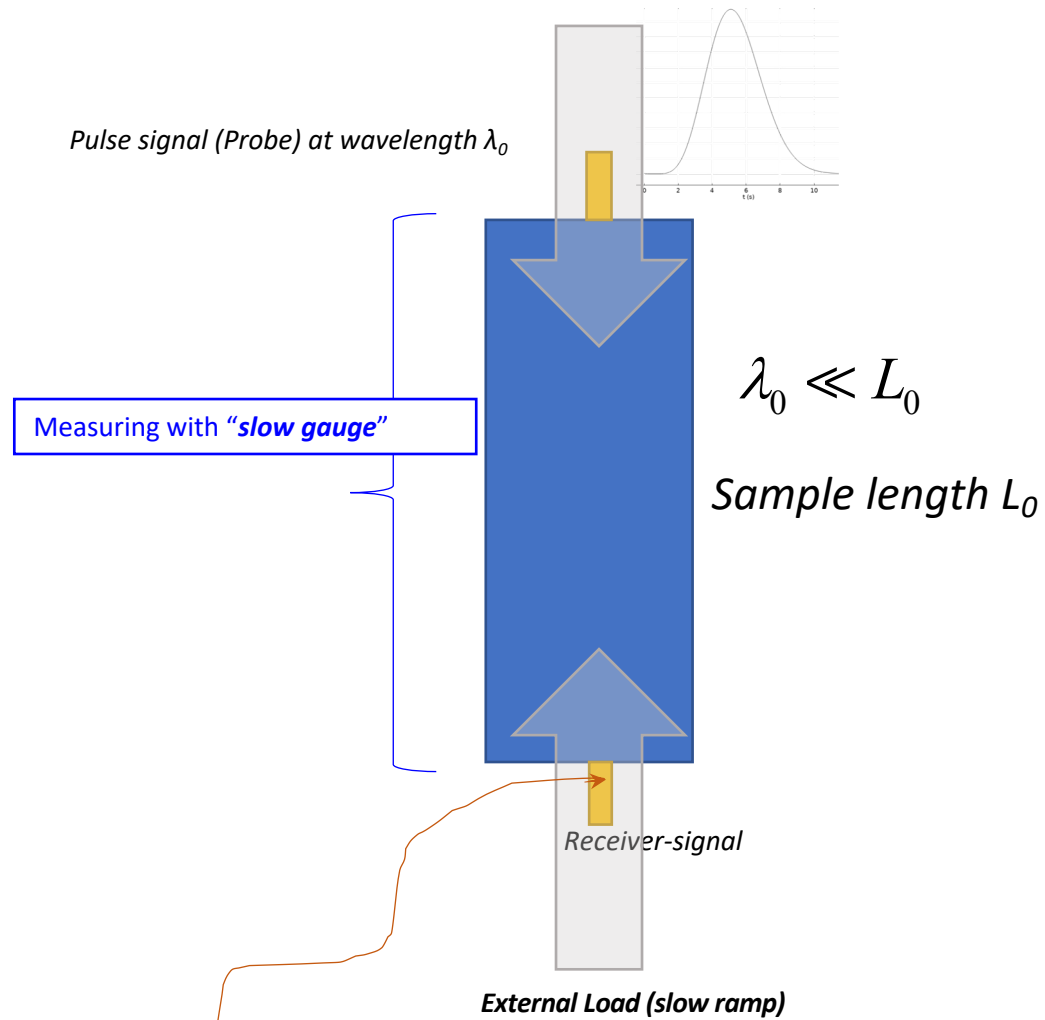
Calcite Samples

- Probing slow deforming energy landscape : **Active (external)probe**



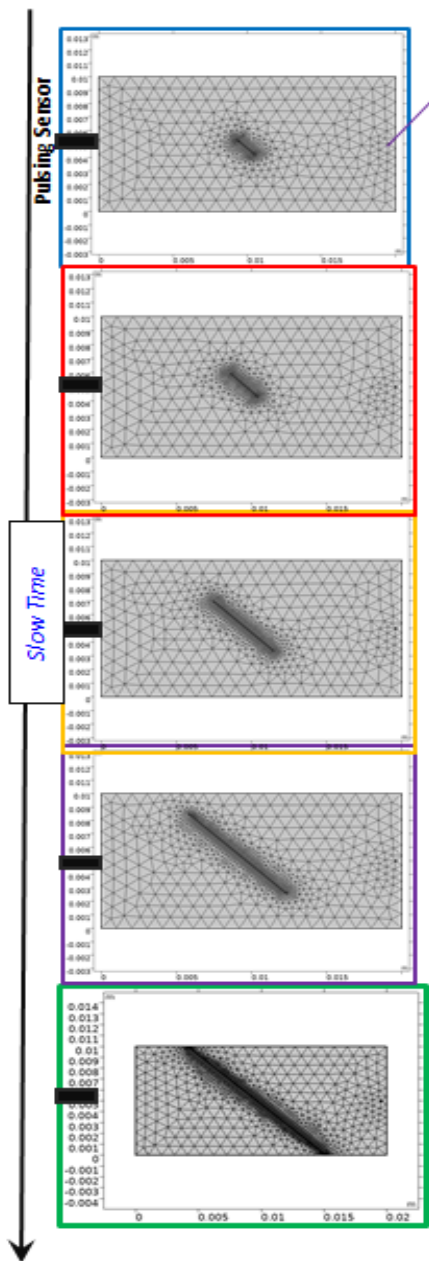
- Special case : **slow deformation** ; non-destructive measure with **fast-probe**

- An example of “fast-slow” time space or “Wave-field” [“Rug Patterns”]

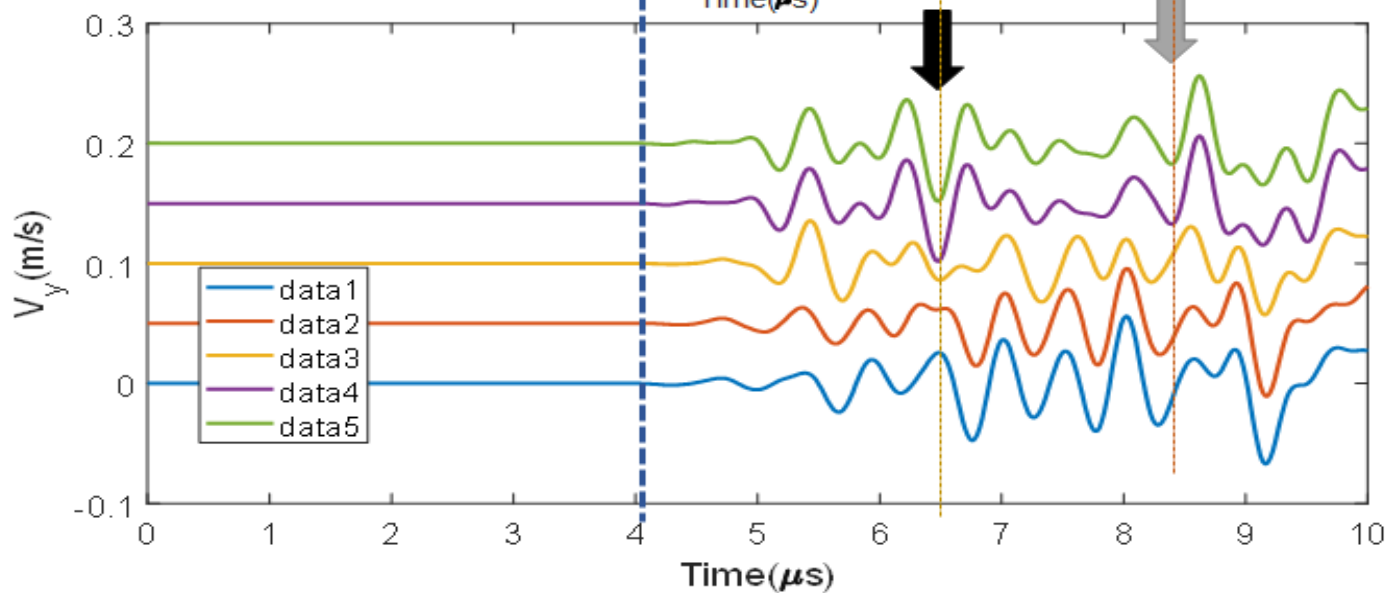
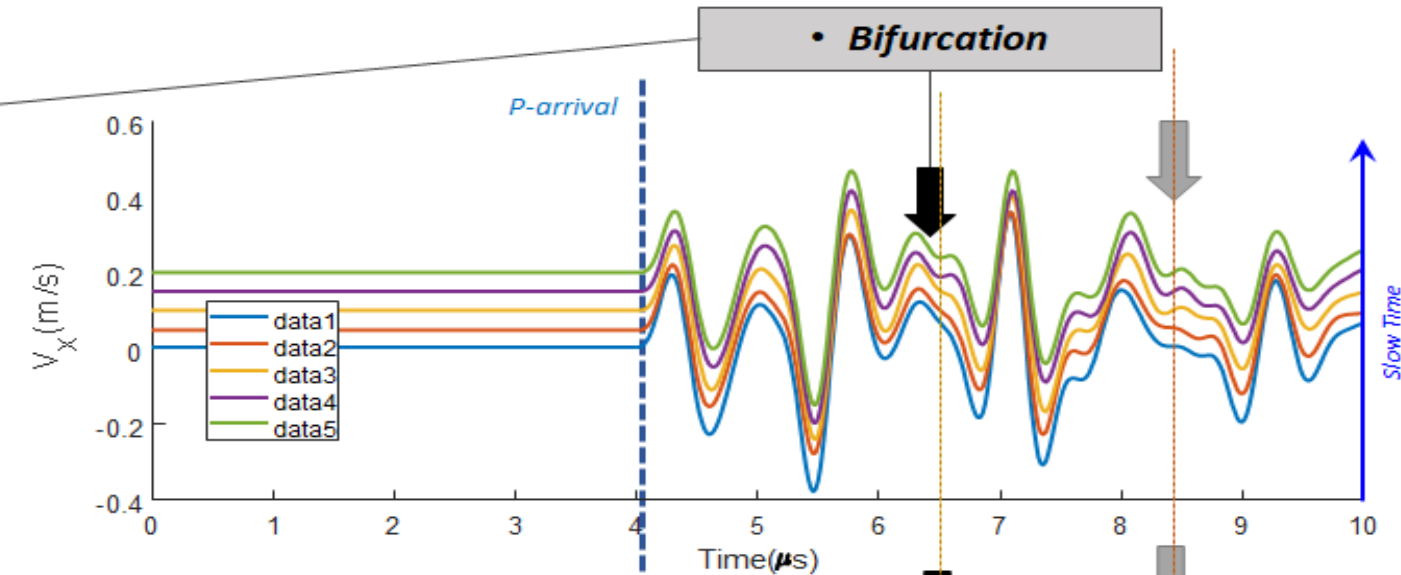
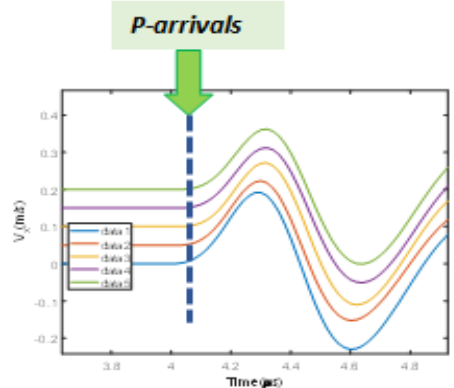
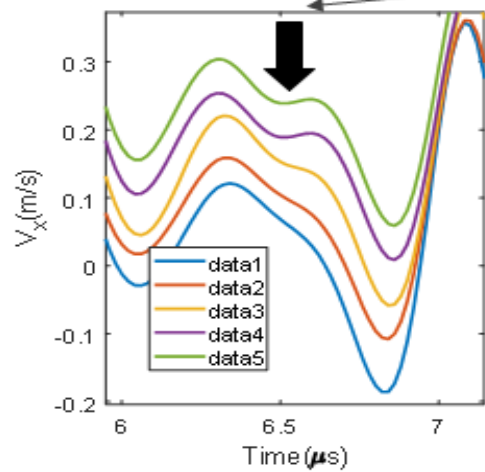


- Fast gauge [=fast response=short response time]

Let's consider synthetic waves...

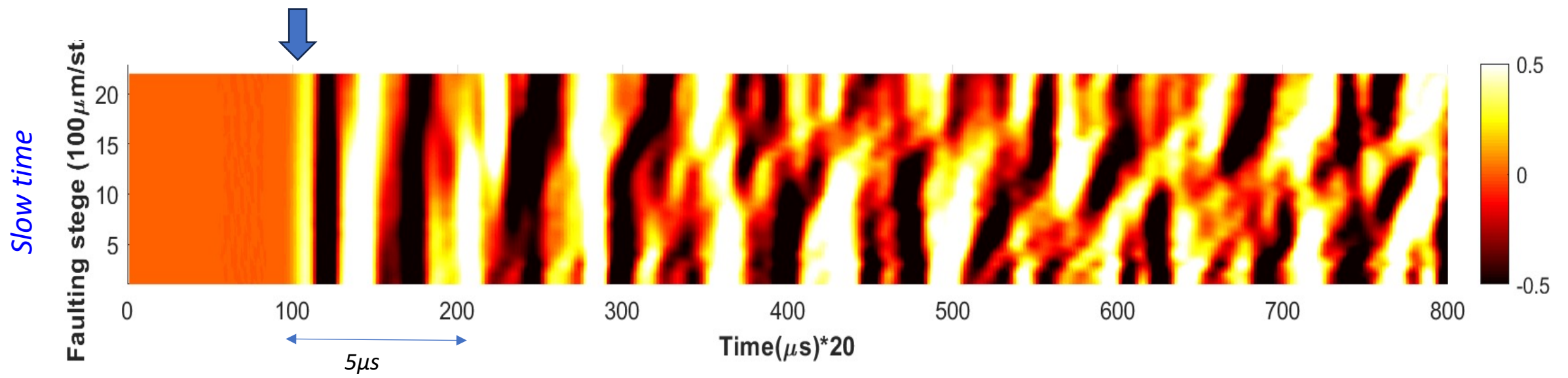
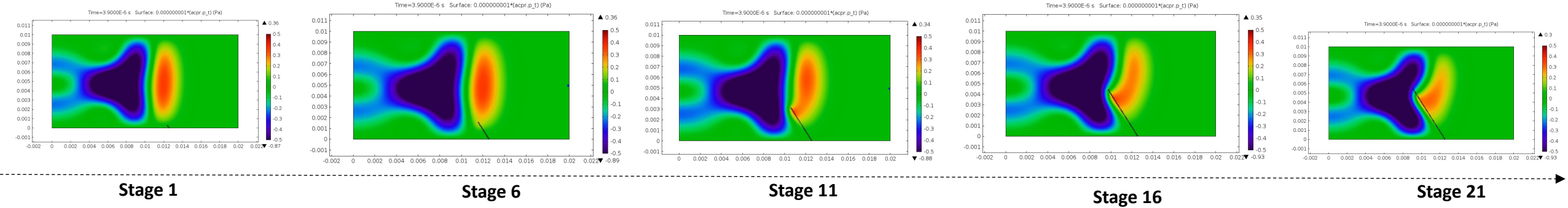


Probe Point



Bi-lateral Propagating of a thin elastic layer

- *Pressure Distribution at $t=3.9\mu\text{s}$*



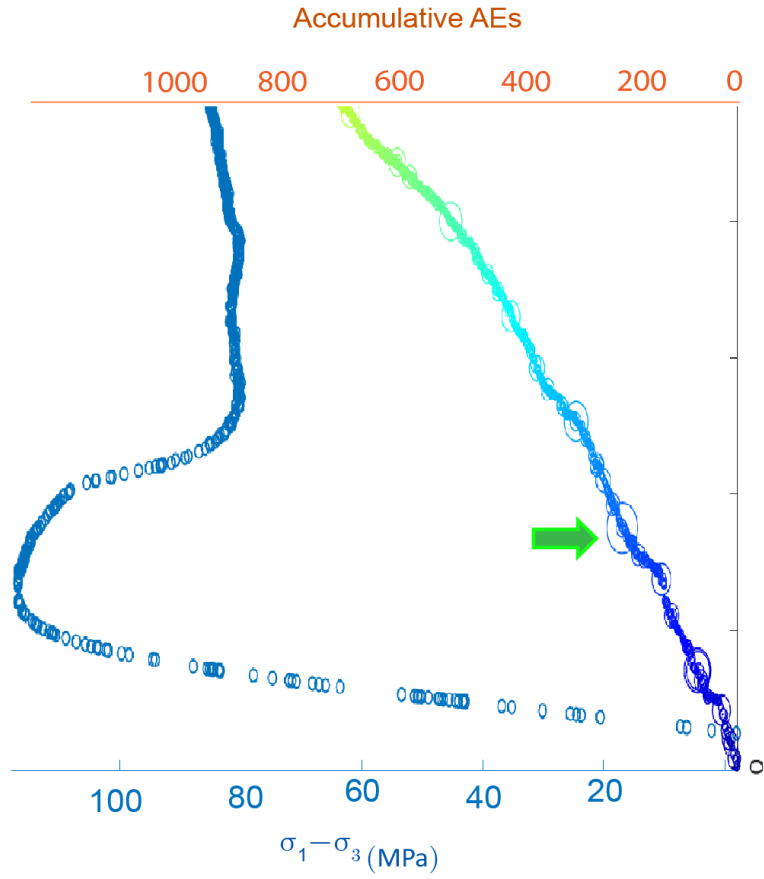
Experimental Observations

*Carrara Marble & Brittle-Ductile transition:
Active fast-slow time space*

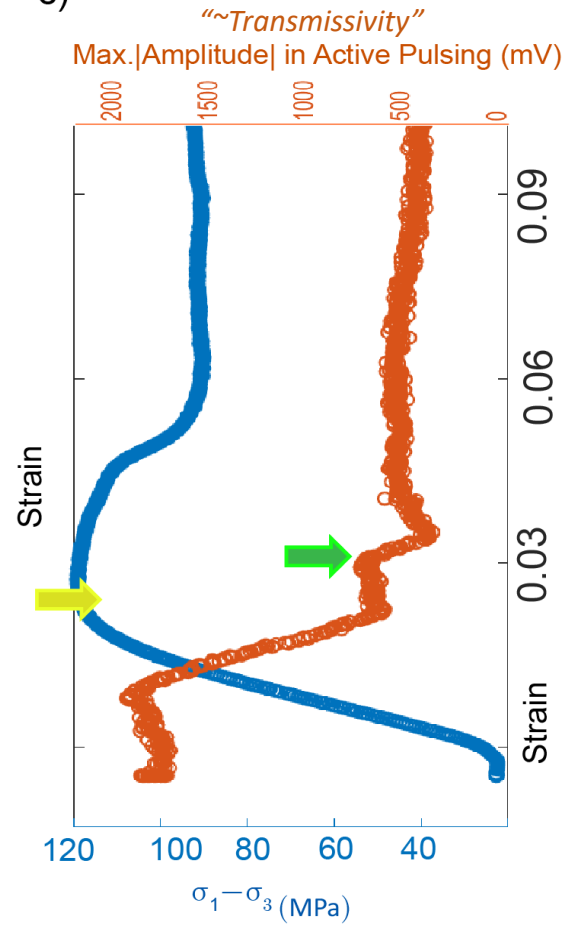
- The configuration of wavefield (“rug patterns of active pulsing”)

Brittle

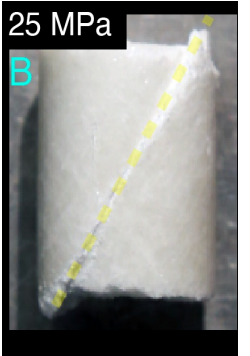
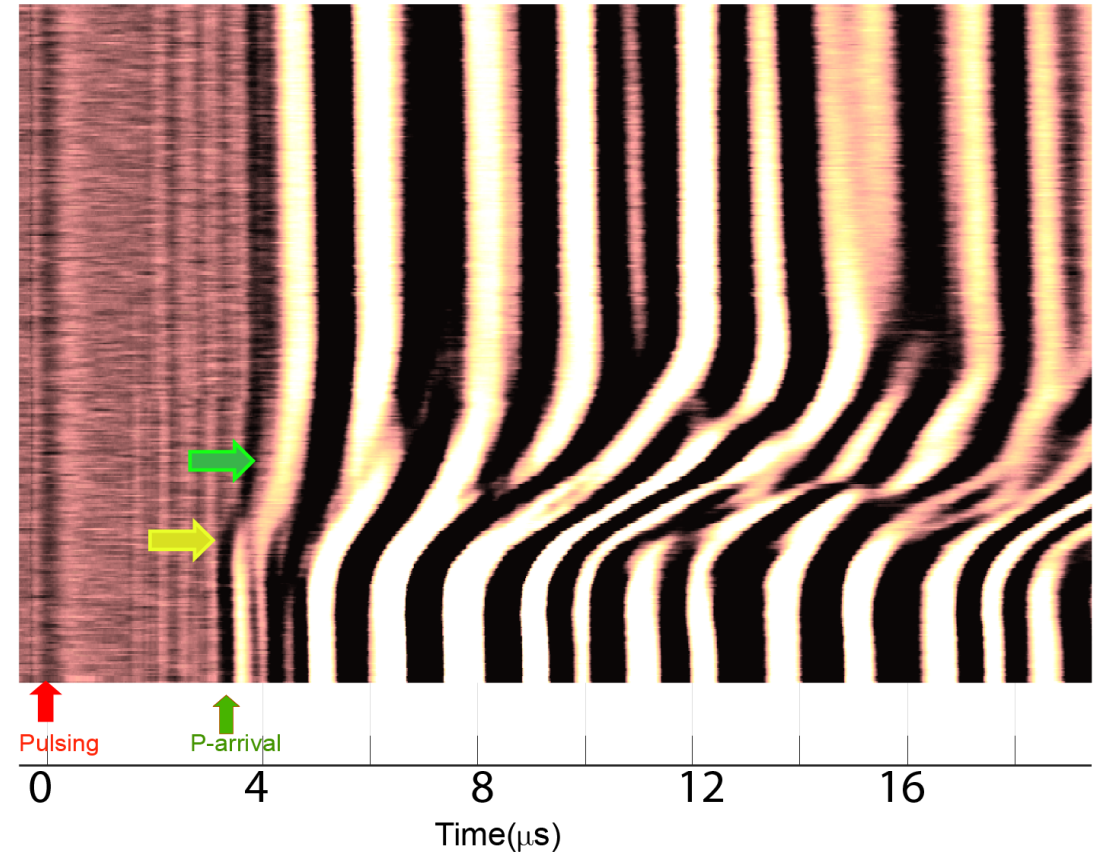
b)

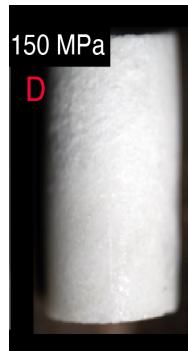


c)

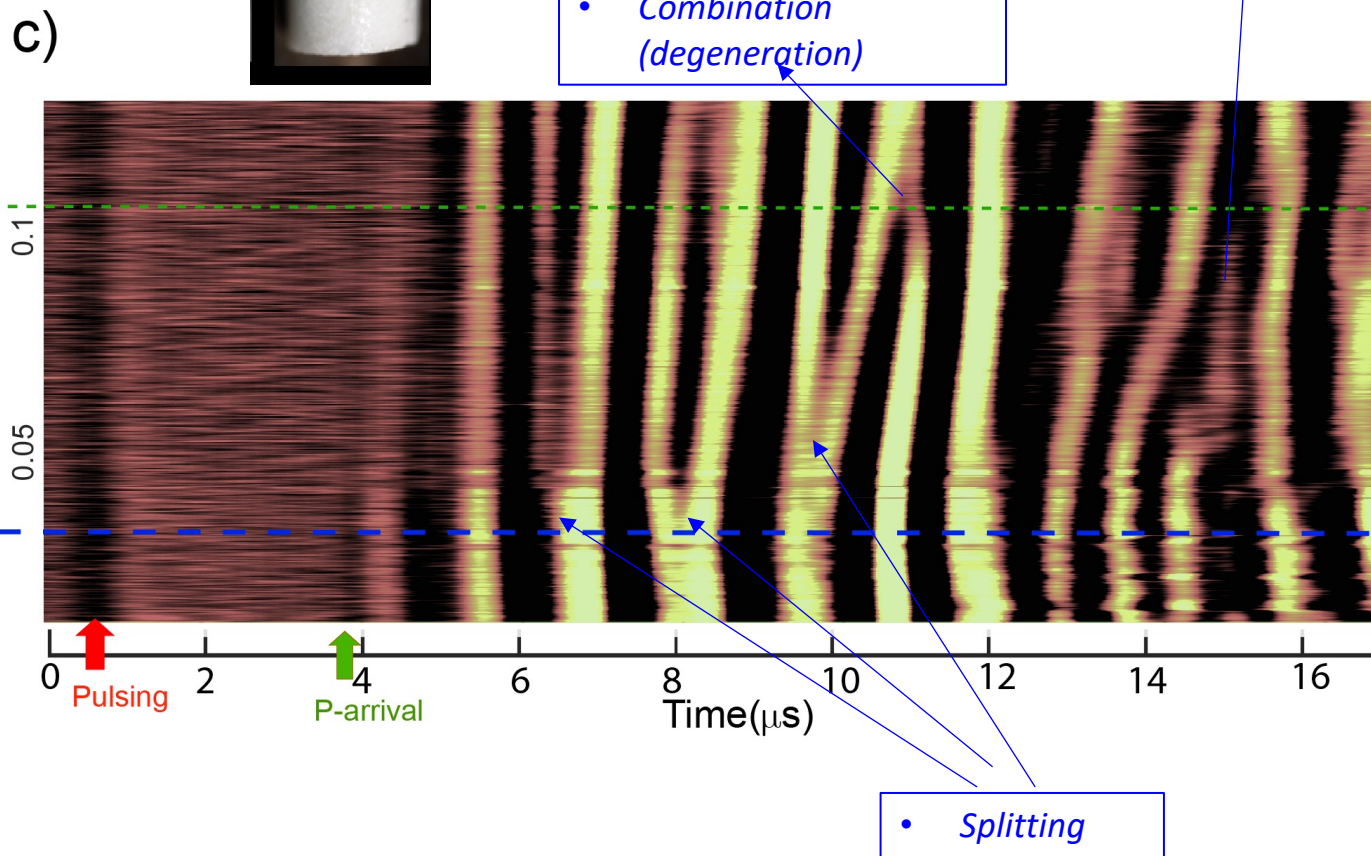
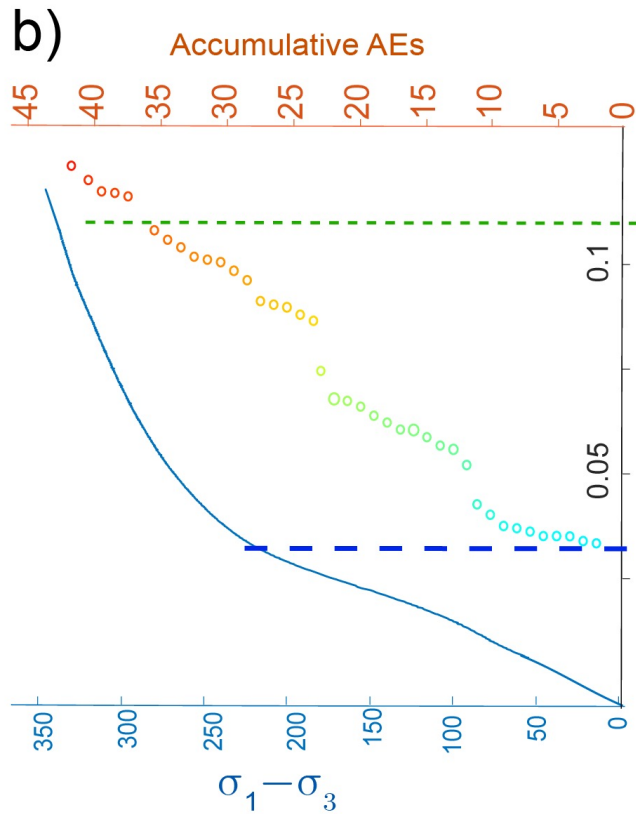
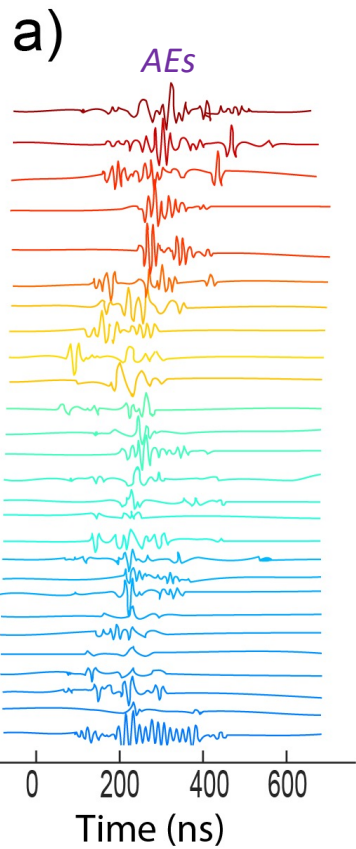


d)





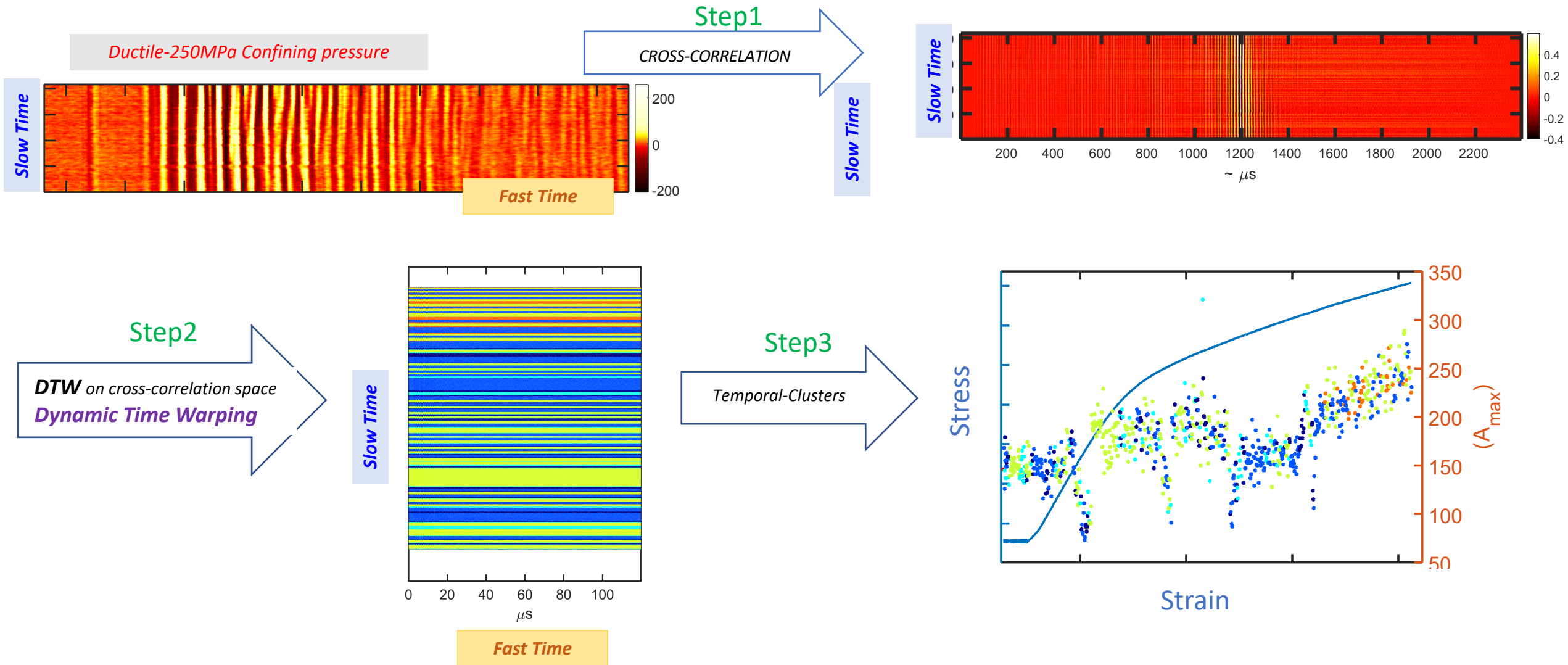
Ductile



Patterns in fast-slow time: Clustering (unsupervised learning)

✓ *Clusters of f - s space unravel the deformation stages (faulting , strain hardening phase)*

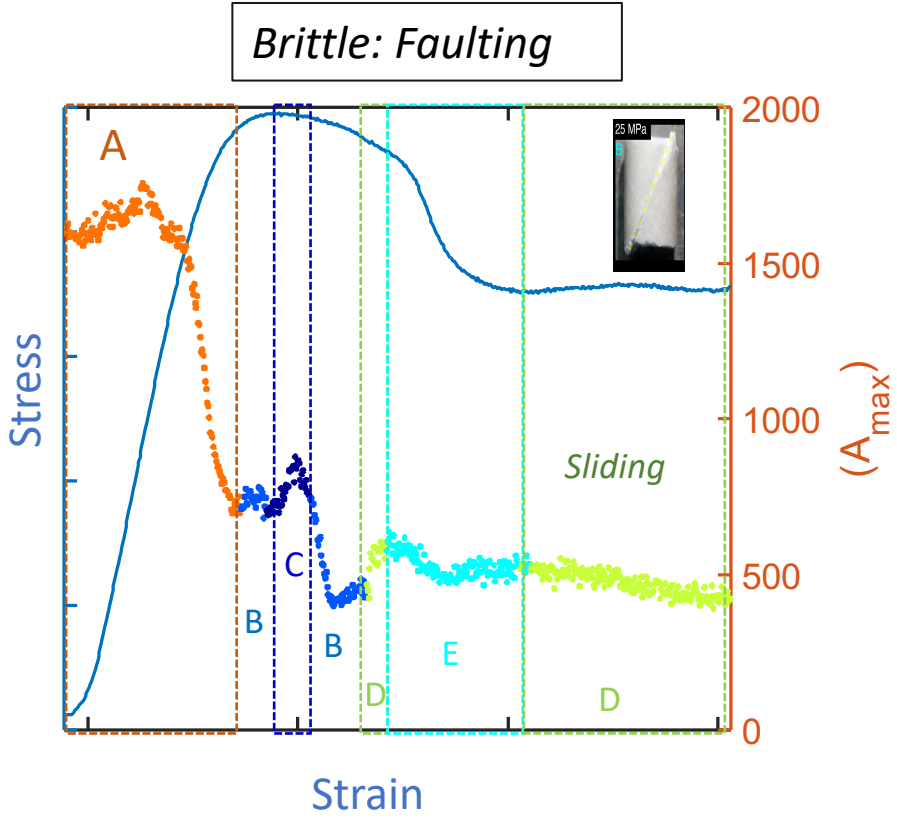
- Deformation of Marble Sample: *clusters* on “Transformed Rug space”



- Clustering (Temporal or spatial) is another manifestation of fast-time
- Evolution of clusters = coupling of fast-slow relaxation times

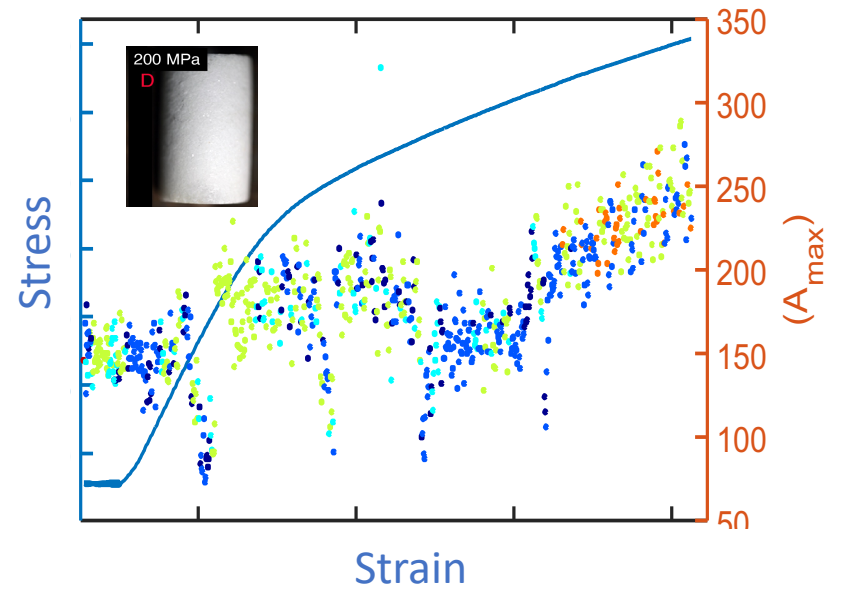
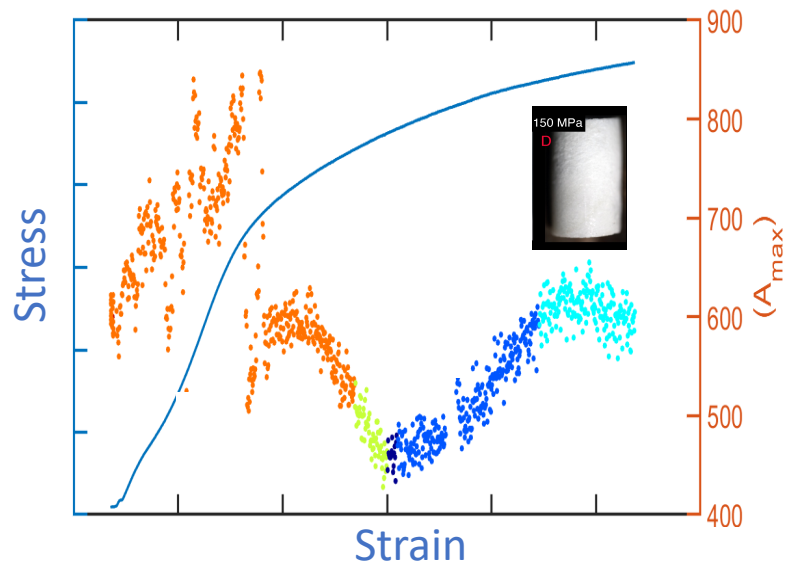
- Classification based on Convolution(cross-correlation)

- clusters of *f-s* space



Brittle-Ductile Transition

Ductile: Strain-hardening

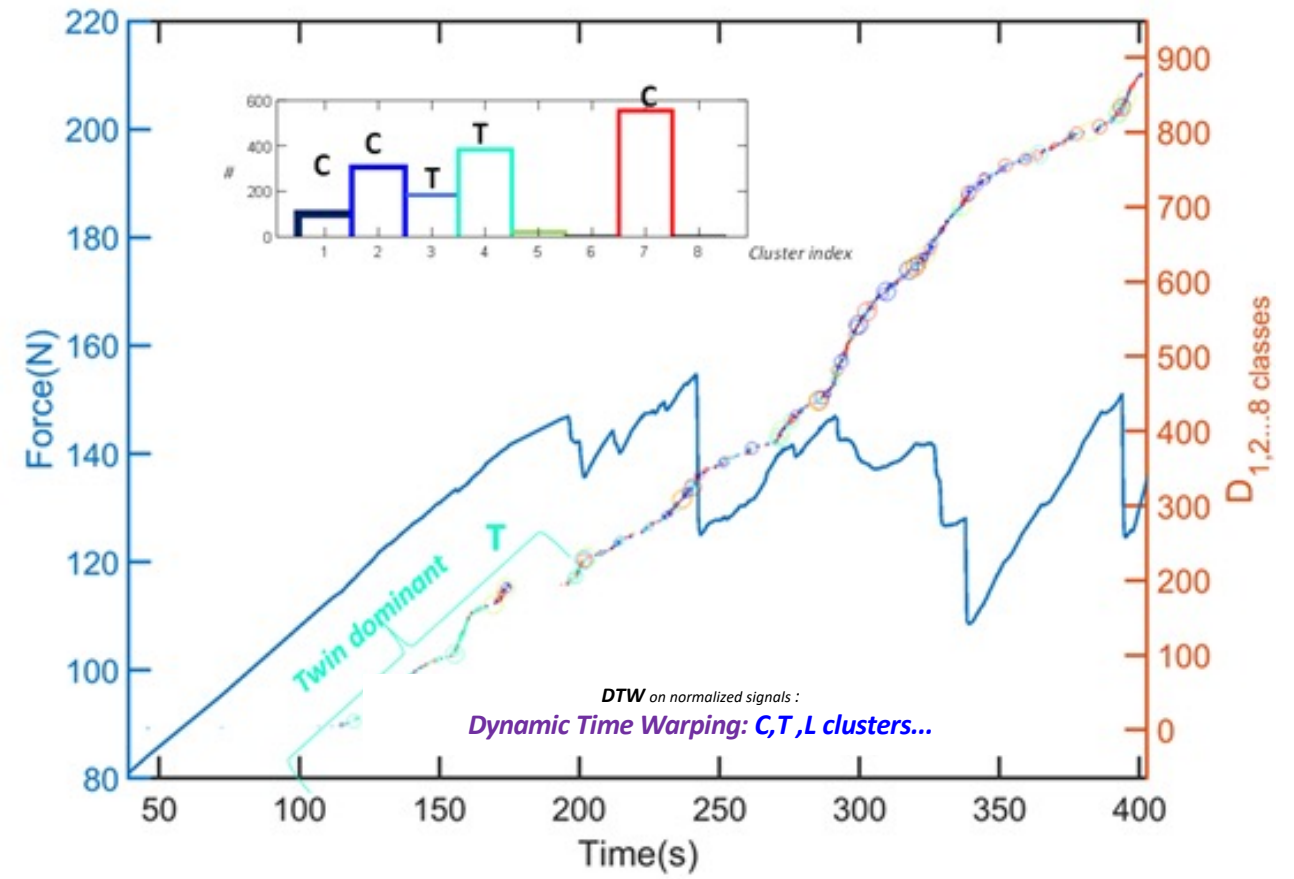
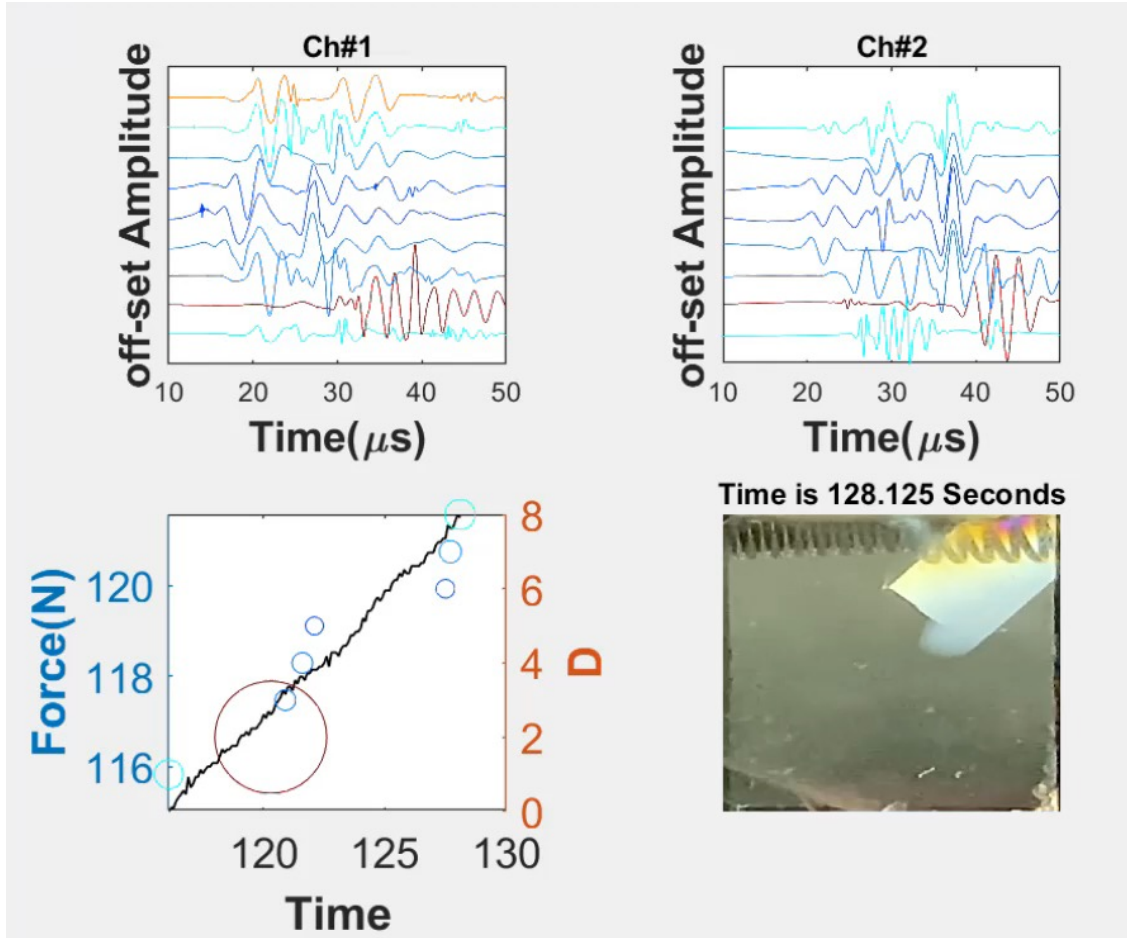


- Clusters of *f-s* space might indicate the deformation stages (faulting, strain hardening phase)

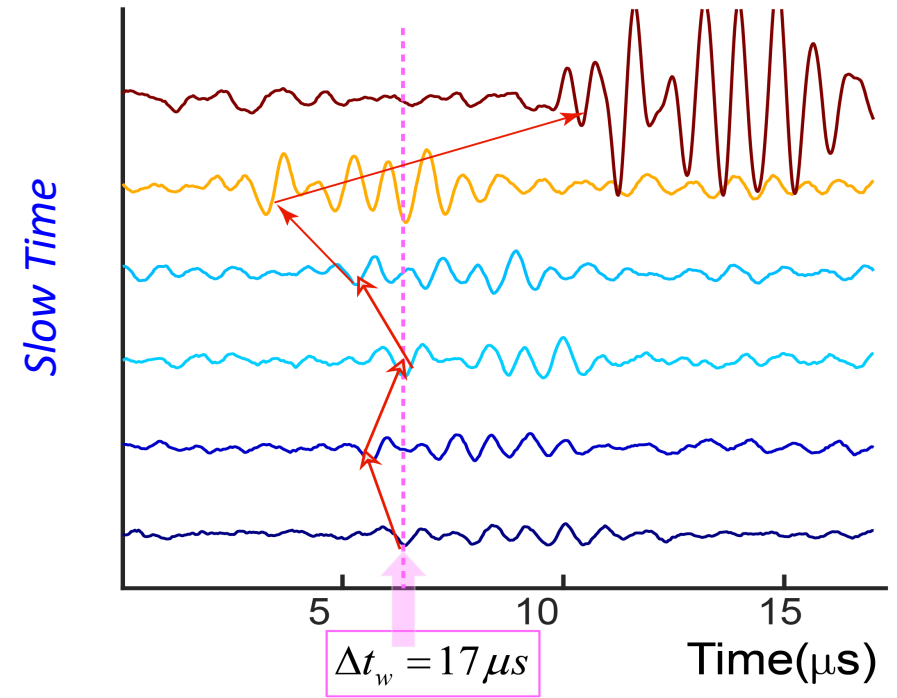
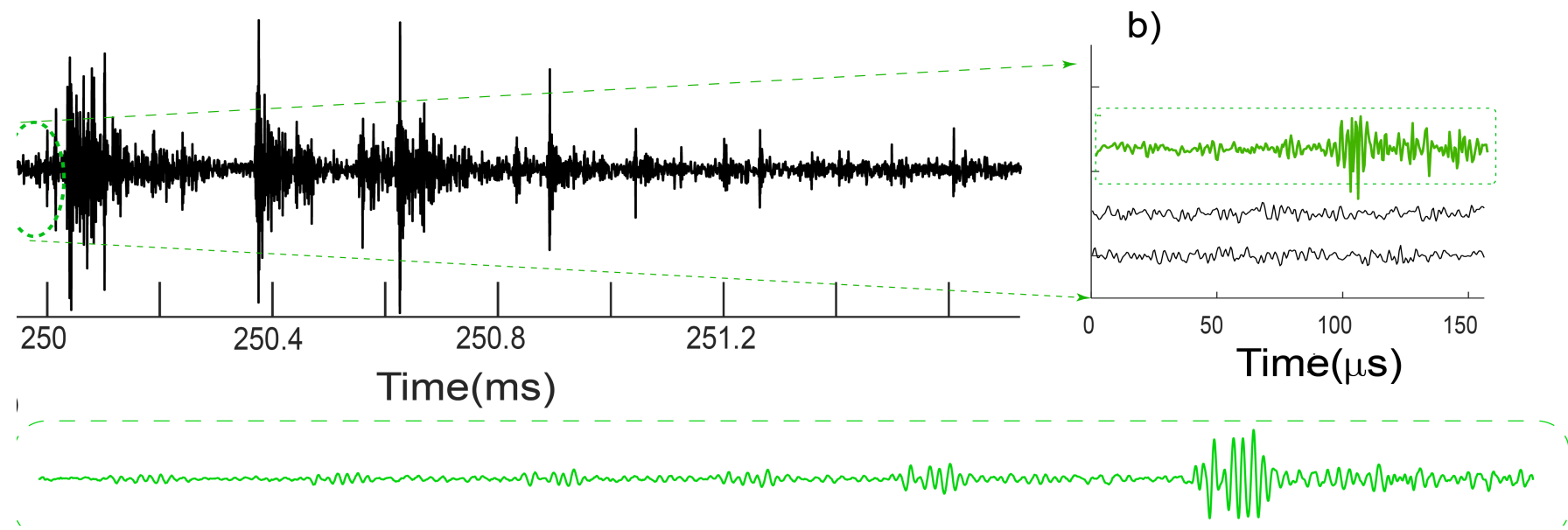
Do we have fast-slow spaces in “passive” excitations (i.e., AEs)?...

- **Clusters of AEs (passive probe) -in slow time (strain, load, etc):**

□ **Each cluster is a flavor of fast-time** : **sequence of clusters in time or space is an indication of spatio-temporal interactions of defects, stress-field evolution and relaxation parameters of the rock**

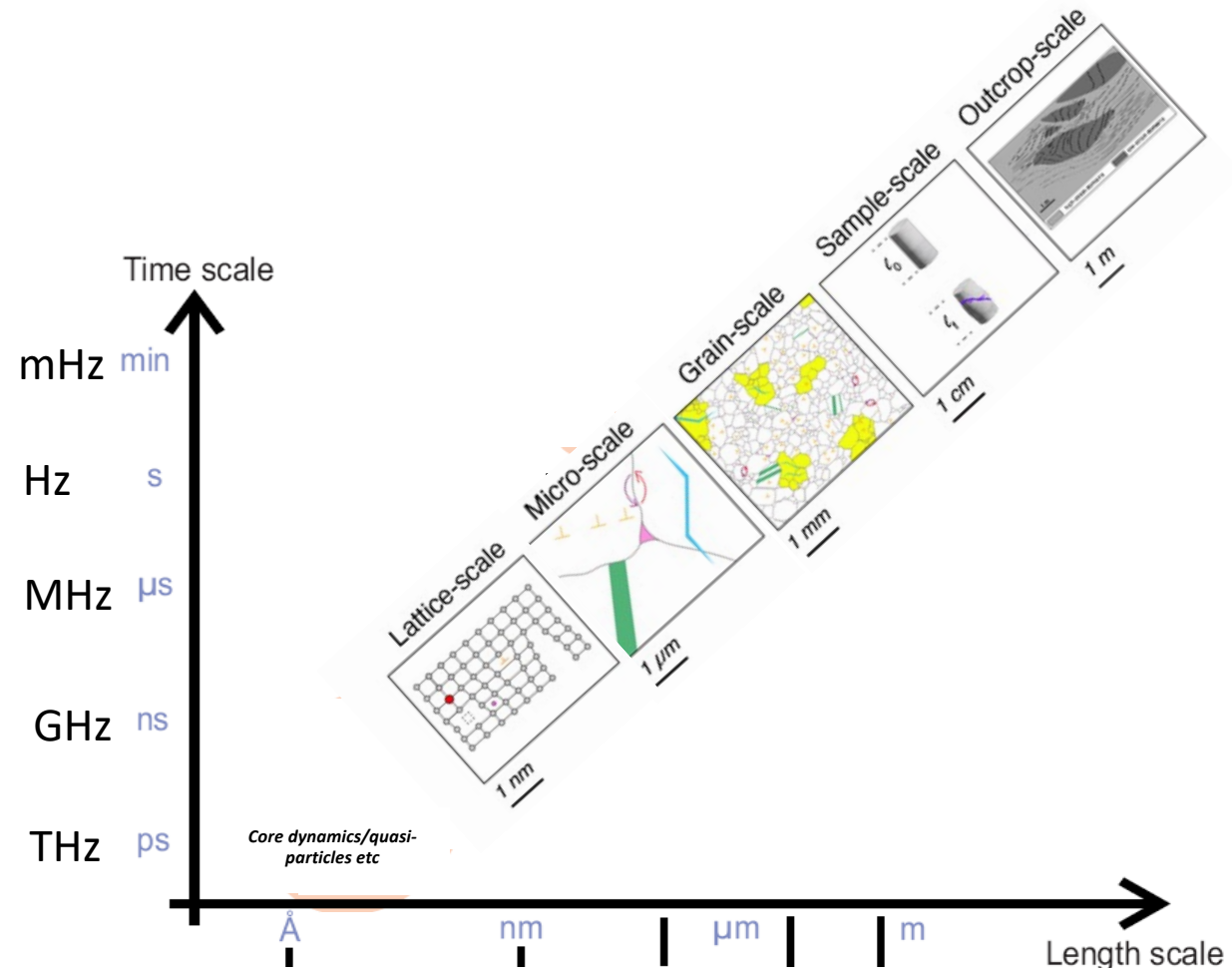


- *Slow Time – ms- from fast time - μ s-: pump is dynamic (source)*

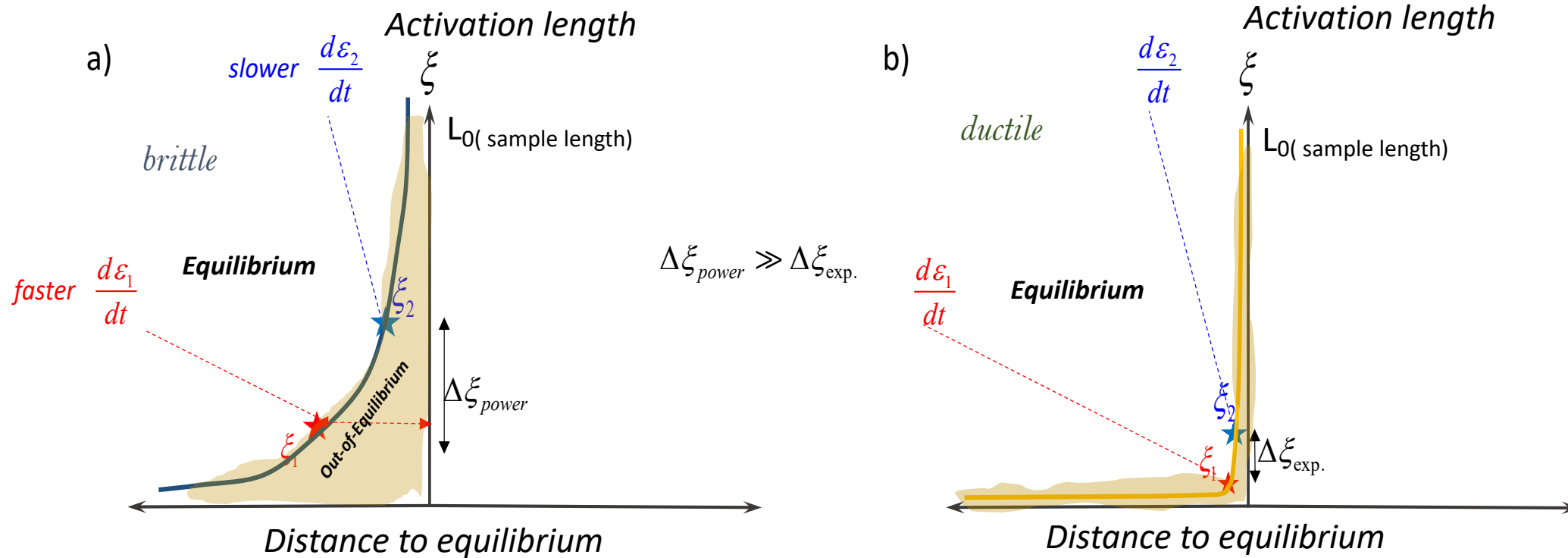


- *Rise of ~constant time-scale*

- Length scalesTime scales : Ladder of scales and building **macro from micro**



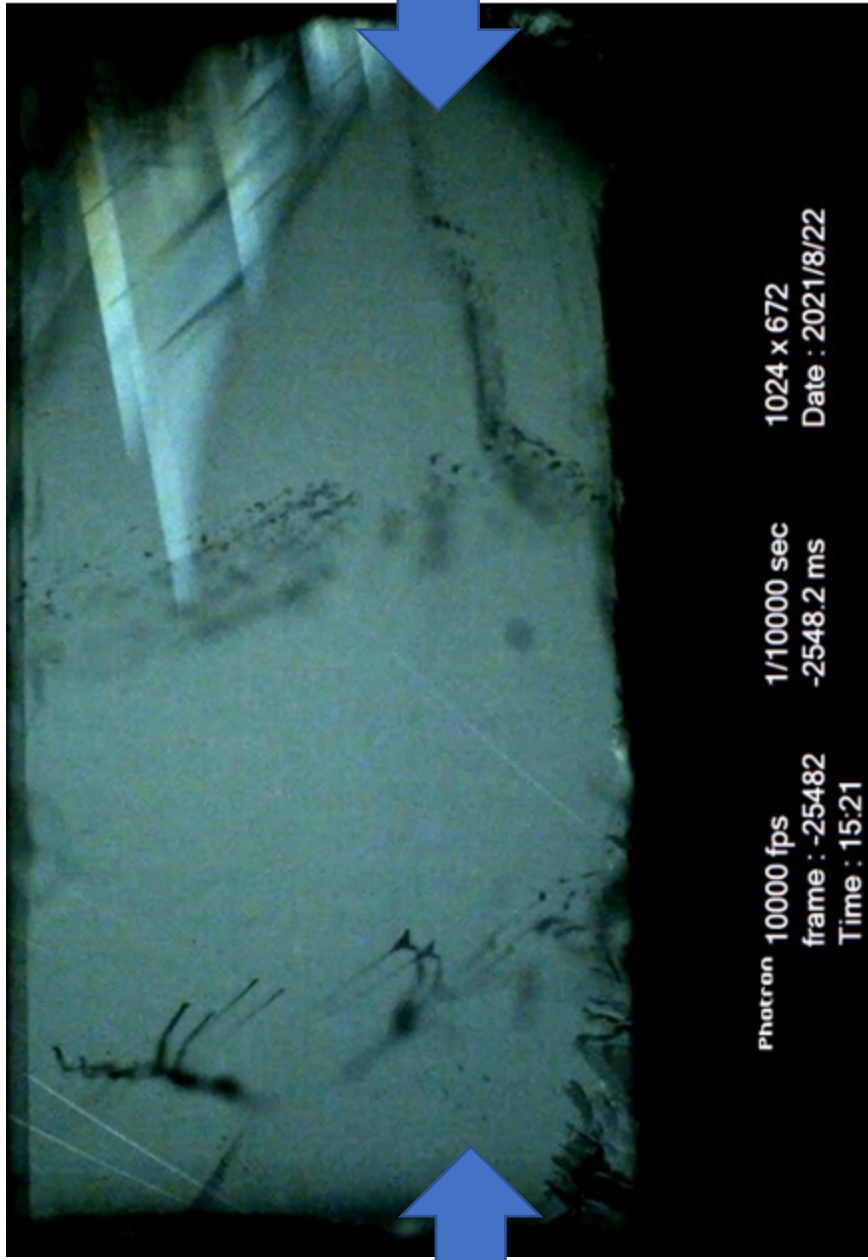
- Rise and Evolution of Defects in different length/time scales : *Dynamic Relaxation Process***



Modified from O'Ghaffari et al, 2016, Scientific Reports
Zurek, 1985, Nature; Kibble, 1976

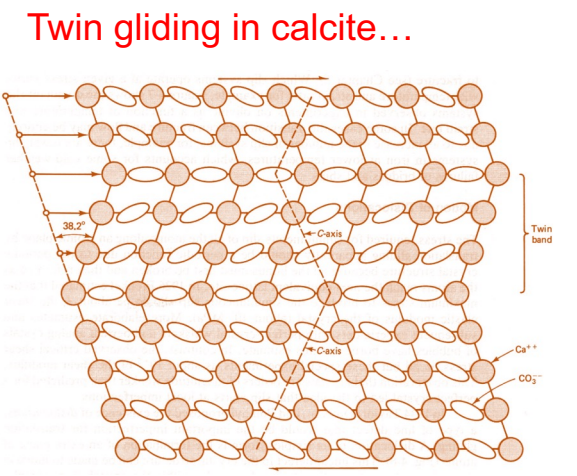
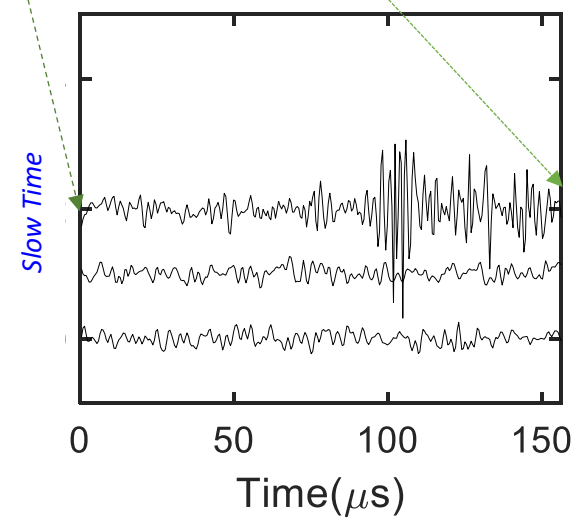
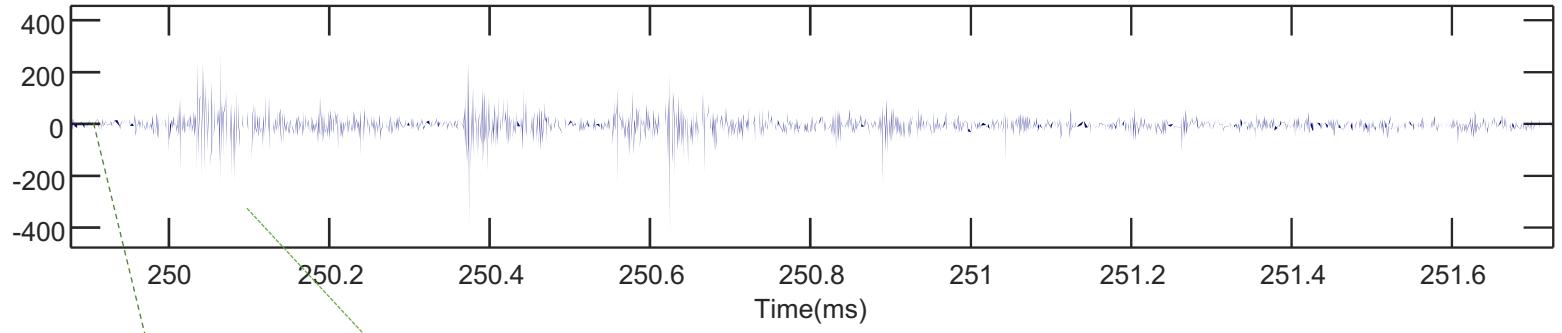
- To have any excitation: one must push the "system" into the *out-of-equilibrium phase (Zurek-Kibble Theory)*
- Energy rate or ramp rate **competes** with equilibrium relaxation
- Time in impulse state (out-of- equilibrium) \sim *duration of an event*
- More resilient relaxation results more uniform impulses states for a given range of energy rates

Questions?

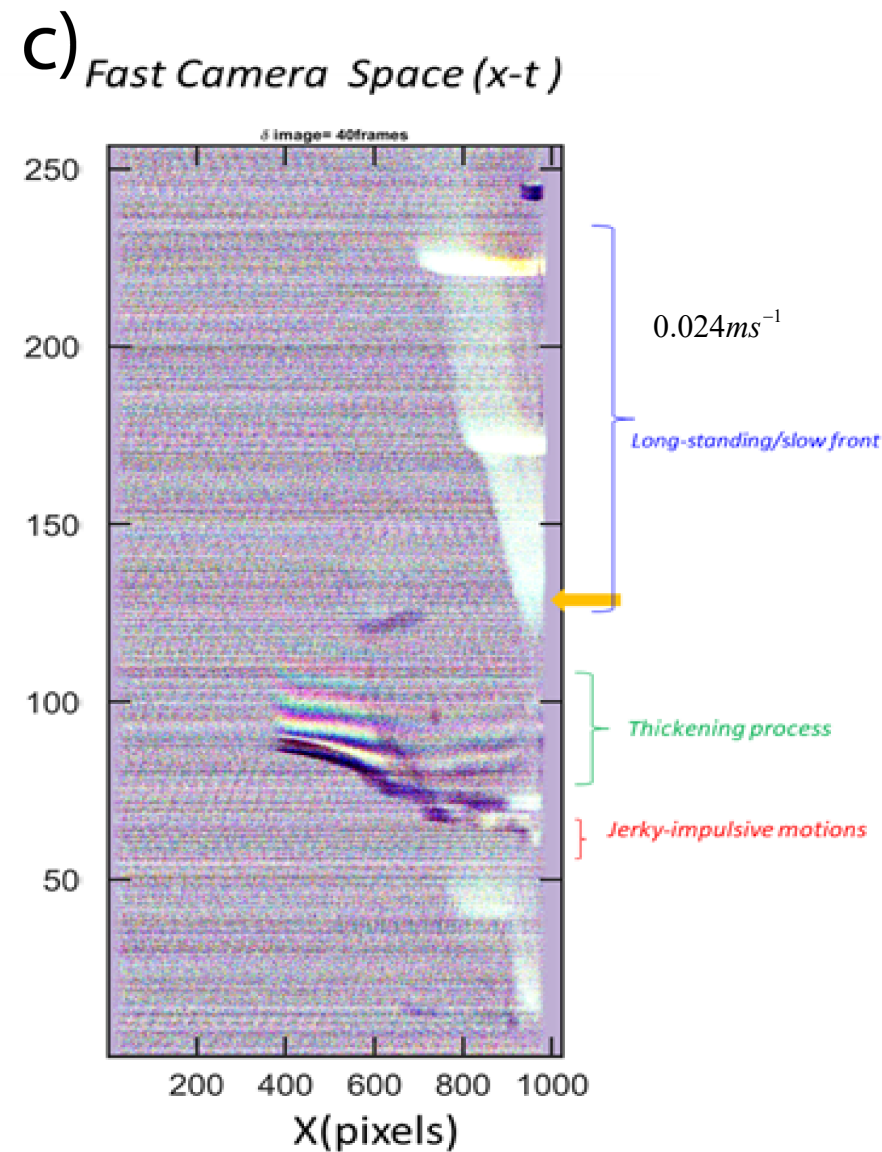
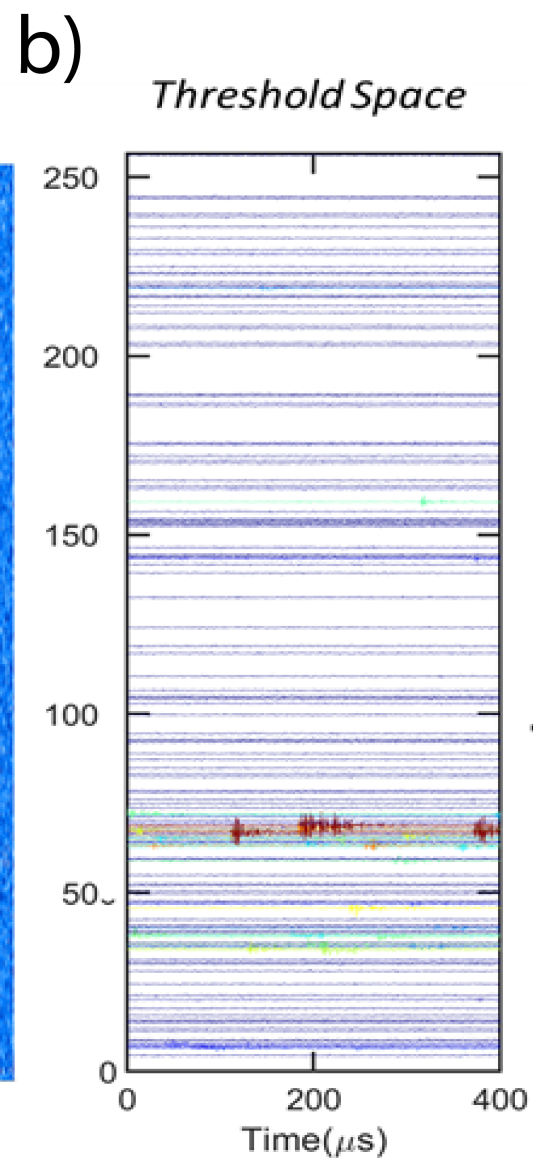
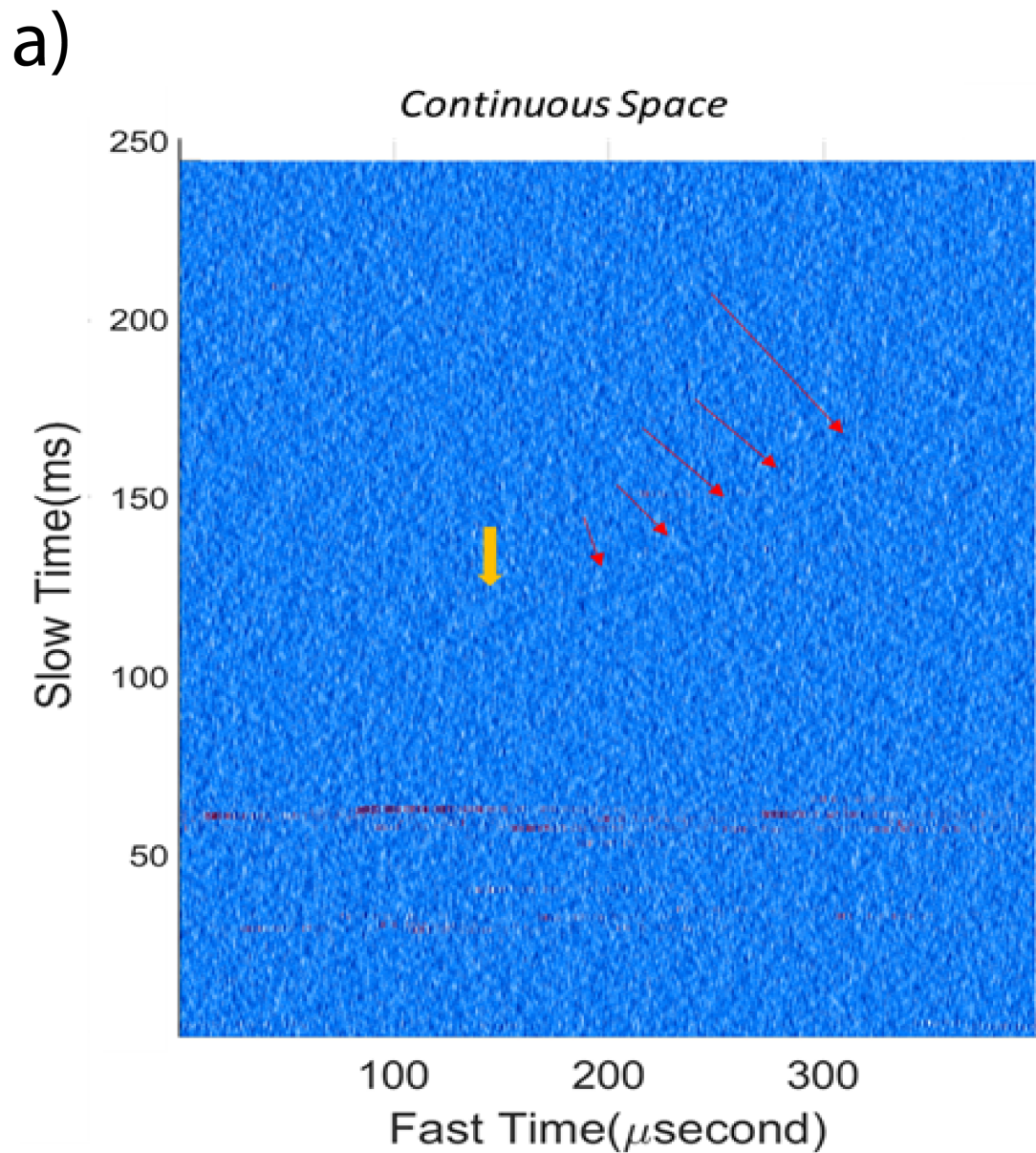


- Twin propagation co-evolving with Thickening process:
- *Shape of a twin (thickness versus length) == fast-slow time manifestation*

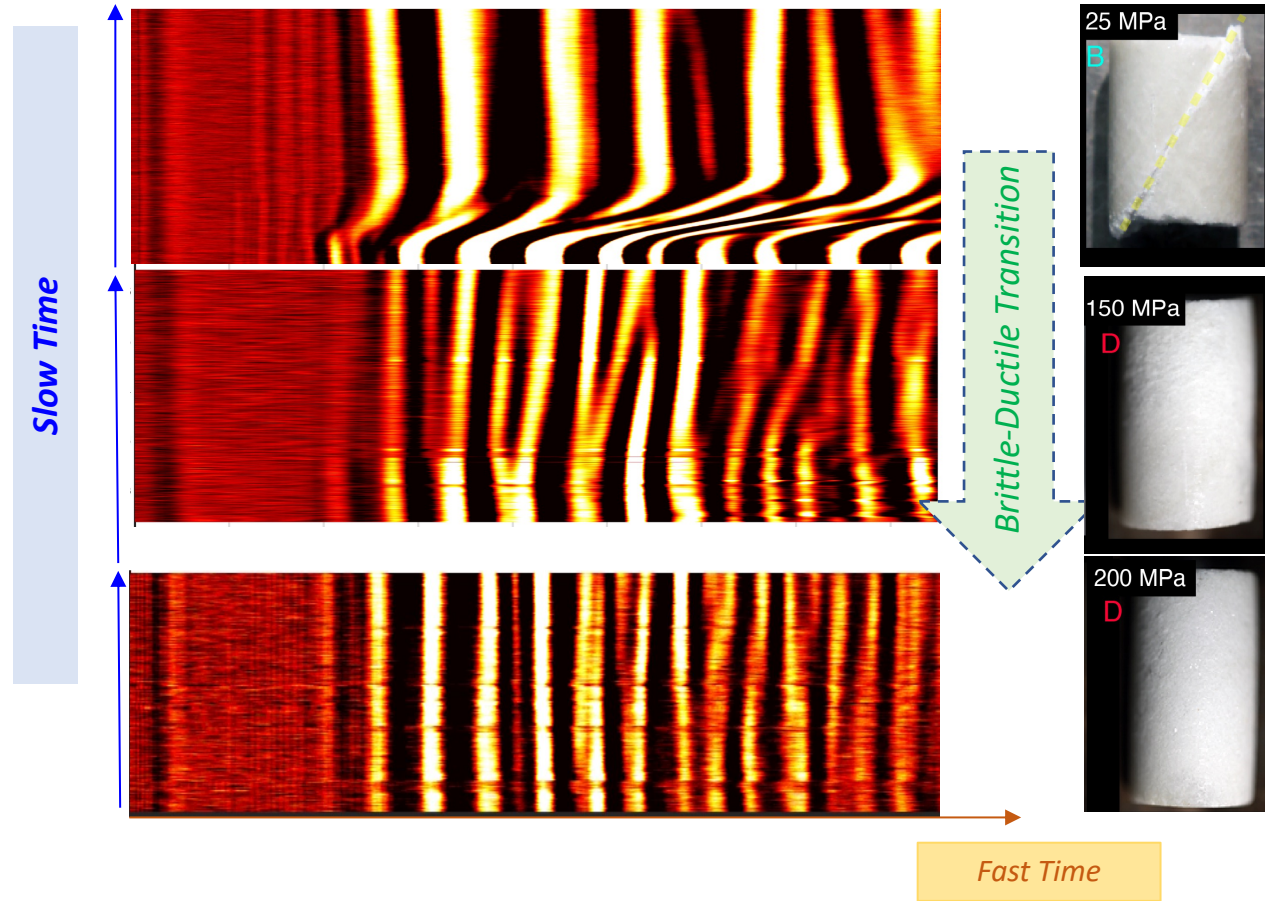
**Now slow Time is ms and fast time is μ s.*



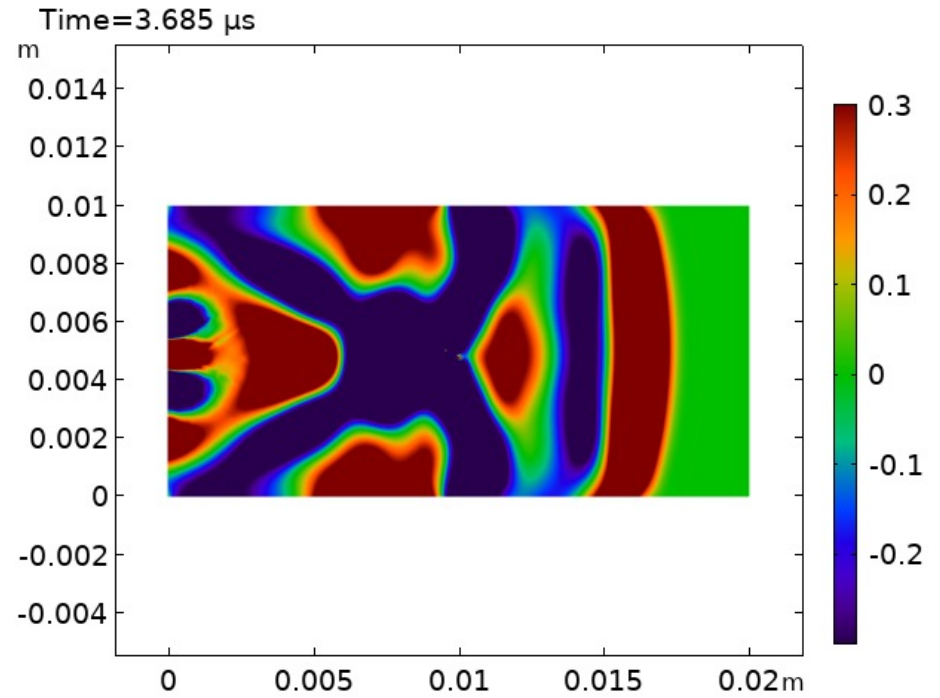
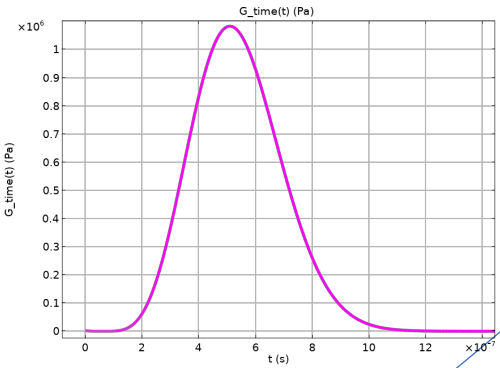
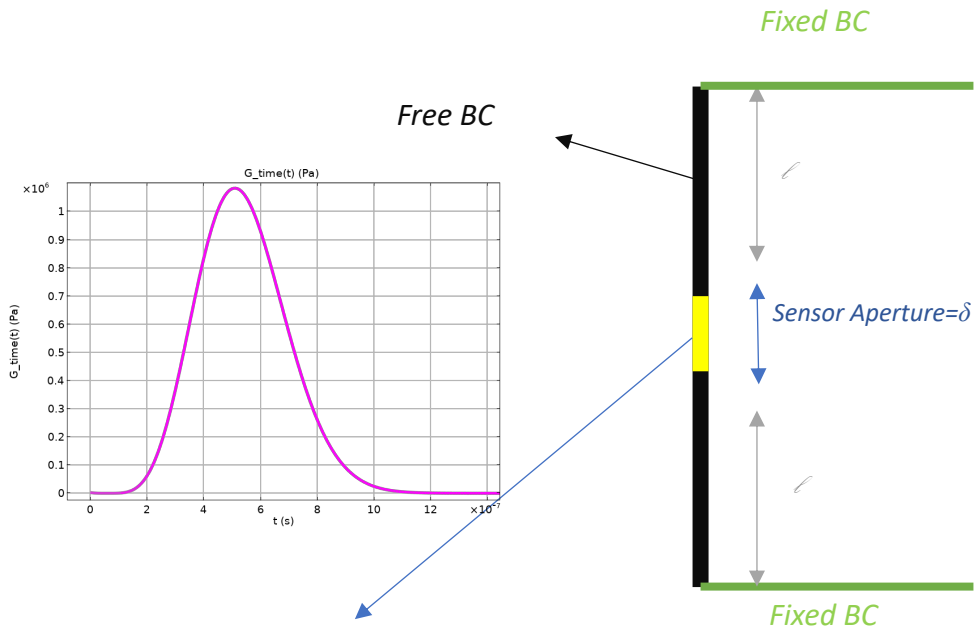
- *Thickening + developing Twin process : The shape of the twin is a manifestation of fast-slow time scales....*



Patterns in fast-slow time...



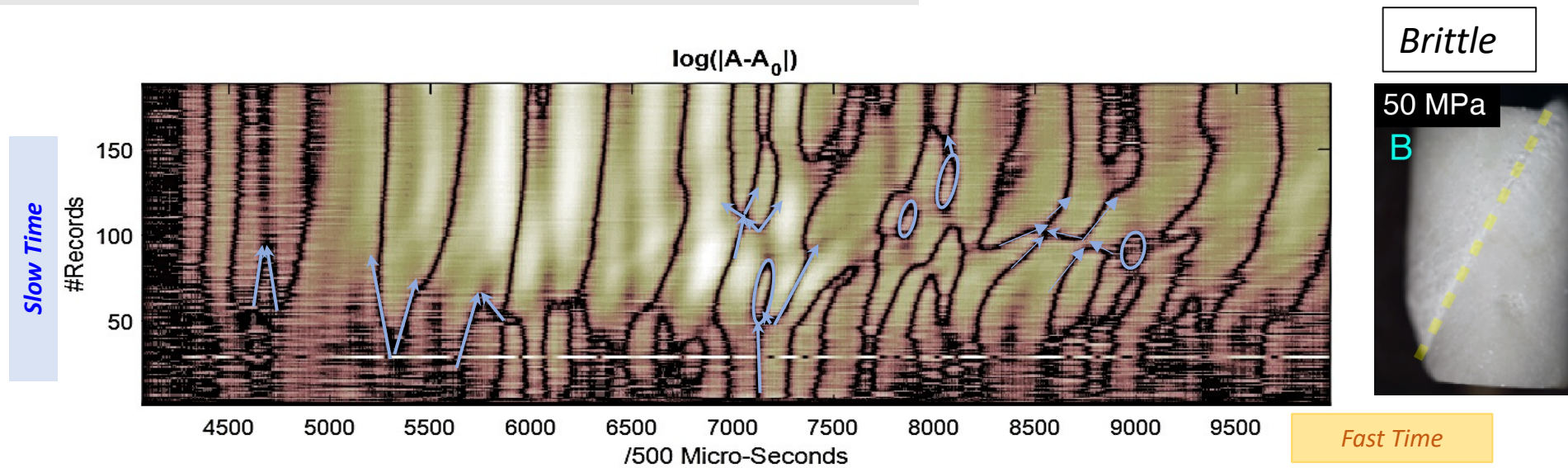
Let's consider synthetic waves...



Vibrating Piezo-wafer(=single Gaussian impulse)

****Zero-crossing objects in f - s space :*
Let's re-consider synthetic waves...

- Deformation of Marble Sample: "Rug" space & Interactions

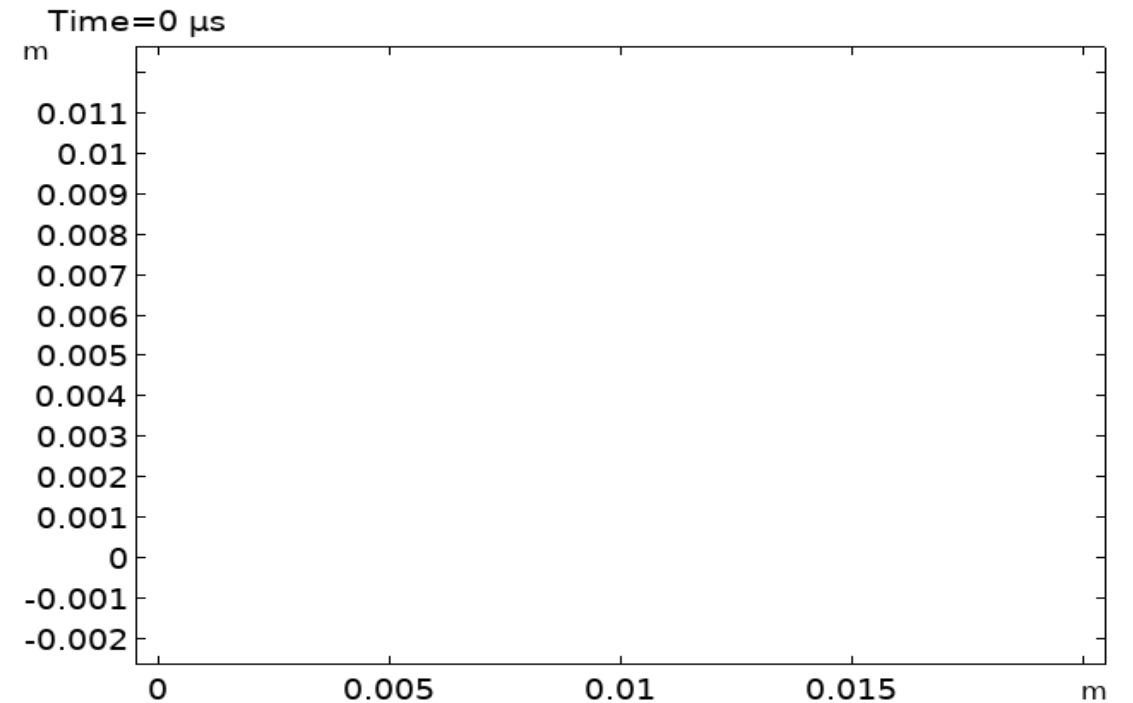
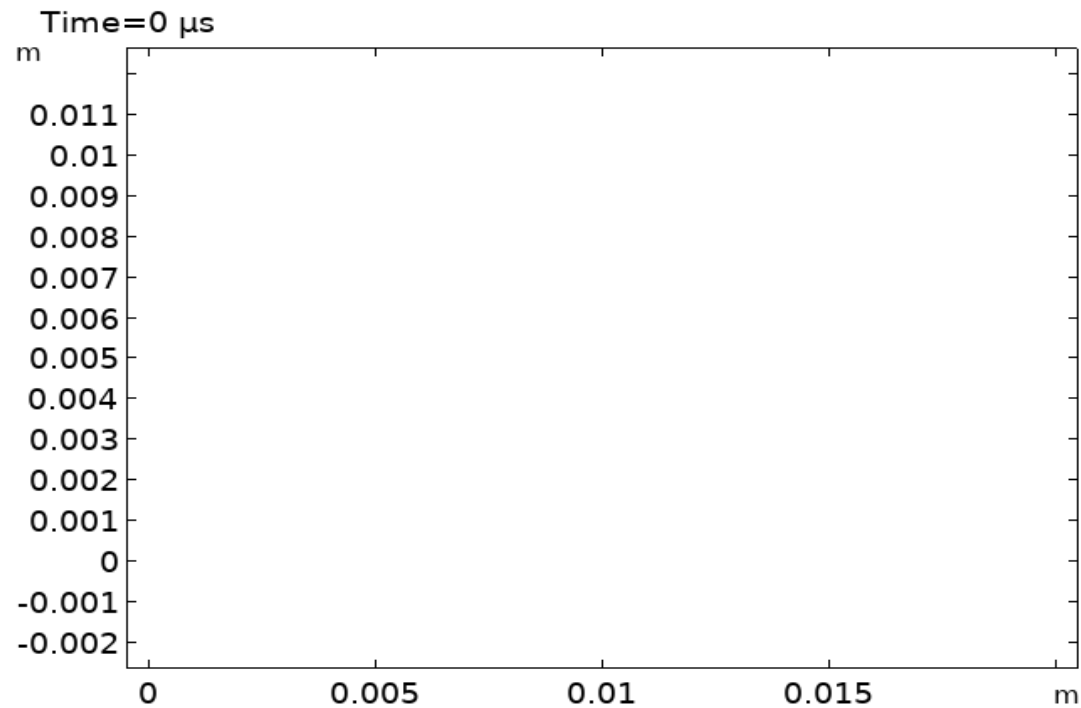


- Rise of Interactions ("Feynman-like Diagrams" in fast-slow space): scattering and wave-wave interactions

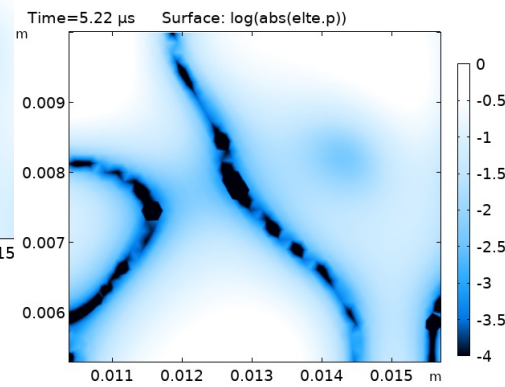
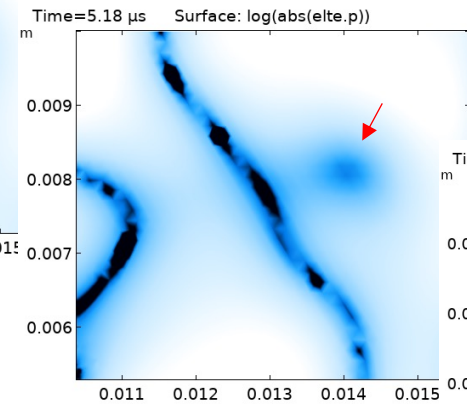
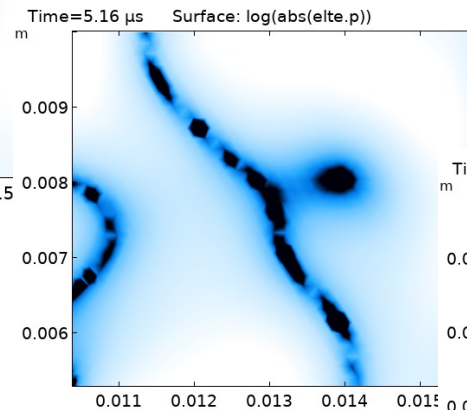
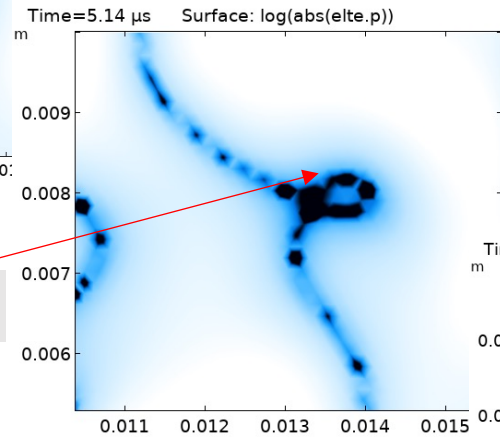
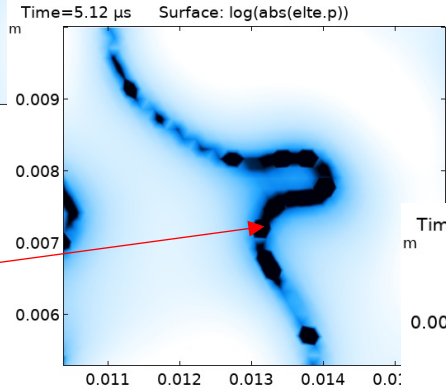
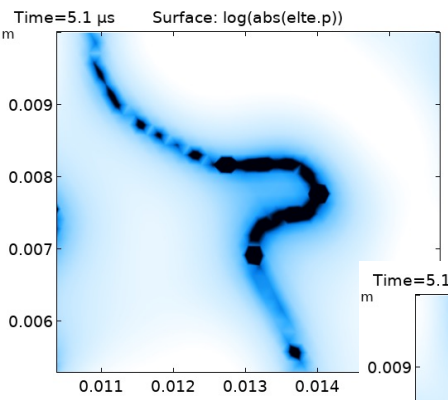
- Zero-crossing domains in X-Y model of *synthetic waveforms* :Pressure field

$$Z = \log | A(t_{[f=0-10\mu s]}, t_{slow} = \text{Fault} - \text{stage2}) |$$

$$Z = \log | A(t_{[f=0-10\mu s]}, t_s = \text{stage3}) |$$



- **Folding/collision and annihilation of zero- “objects” or “strings”**

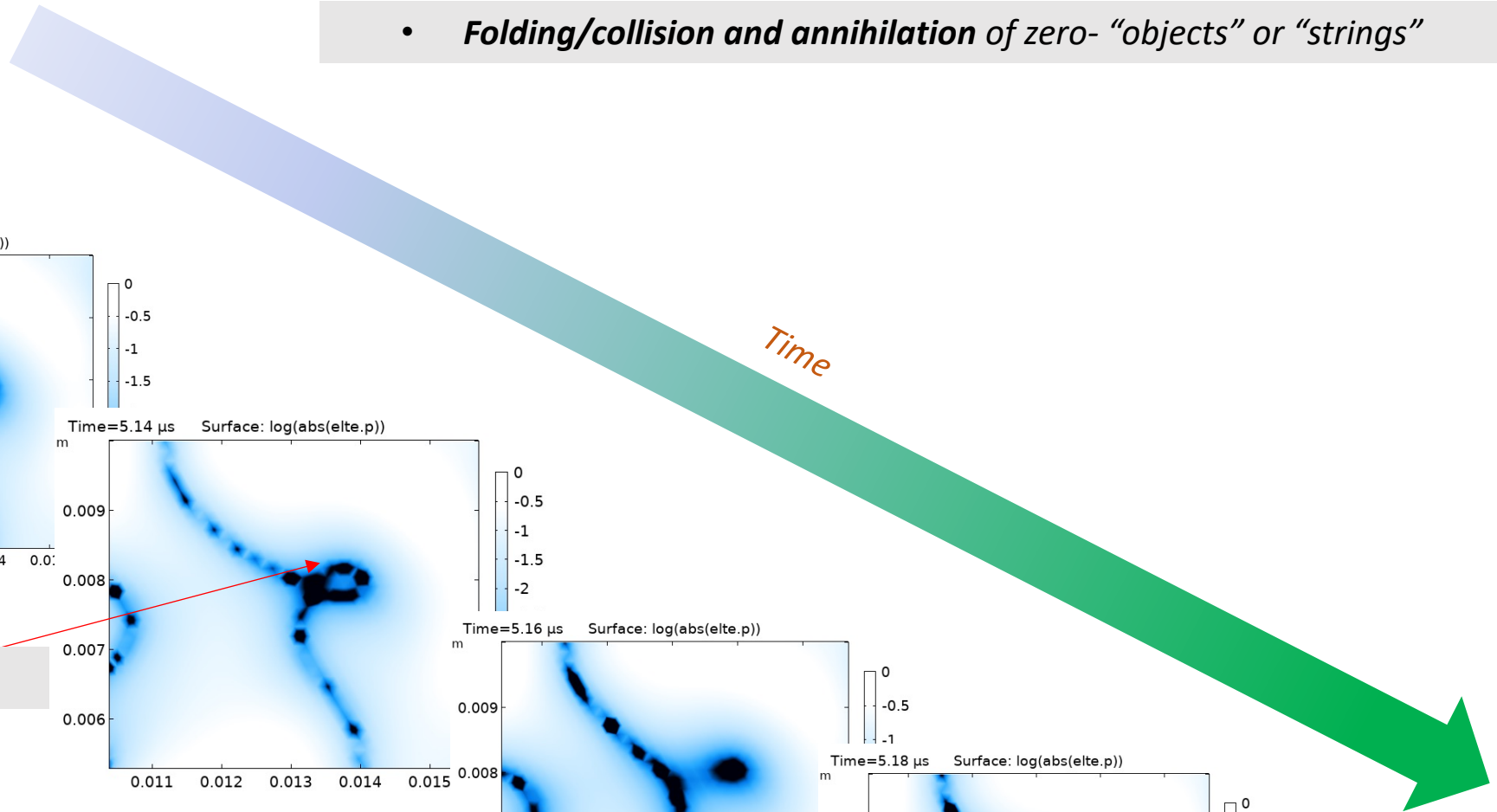


...More Curvature
and bending:
... folding

➤ formation of isolated “bubble”

➤ The isolated loop is annihilating

$$\Gamma_{p \approx 0}$$

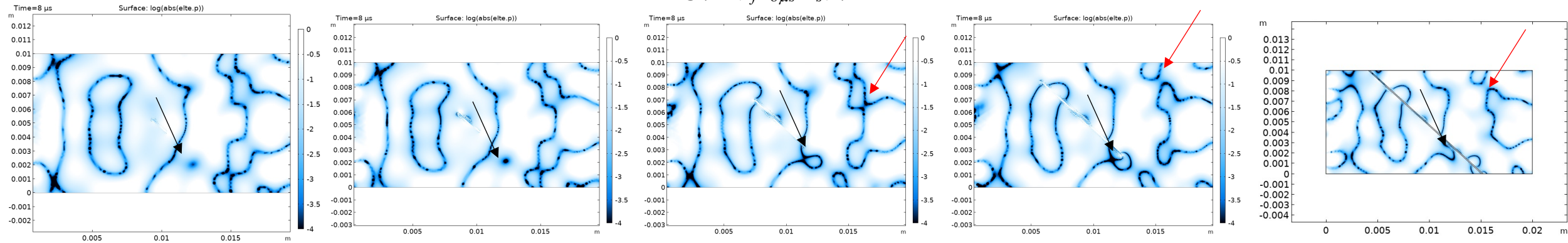


- Interactions of Zero-pressure domains

- Example in X-Y model of synthetic waveforms : Pressure field

- ..let's evolve the slow time with increasing fault length but freeze "fast-time"

$$Z = \log | A(t_f=8\mu s, t_s) |$$



$t_s = \text{stage1.5}$

$t_s = \text{stage2}$

$t_s = \text{stage2.5}$

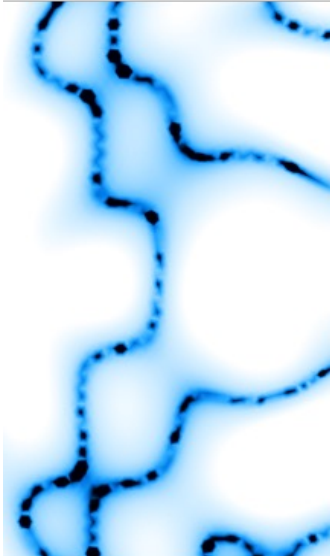
$t_s = \text{stage3}$

$t_s = \text{stage4}$

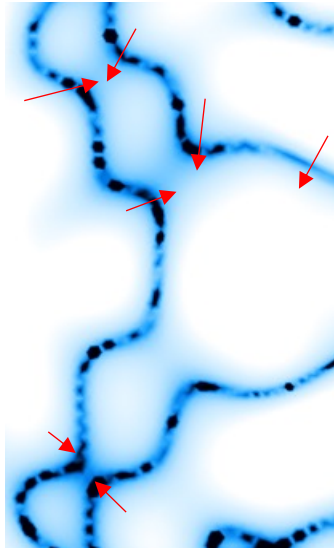
Slow Time=Faulting stages

- **Stages of faulting** & Zero-crossing objects

$$\Gamma_{p \approx 0} \quad Z = \log | A(t_{f=8\mu s}, [t_s]) |$$

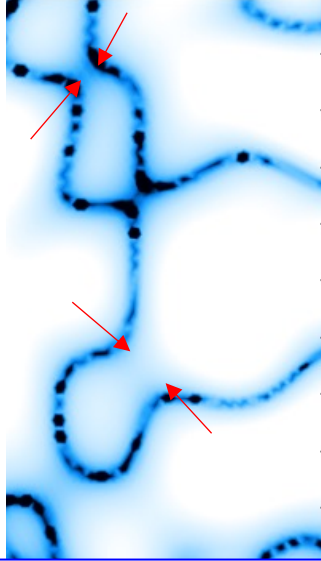


$t_s = \text{stage1.5}$



$t_s = \text{stage2}$

Attraction

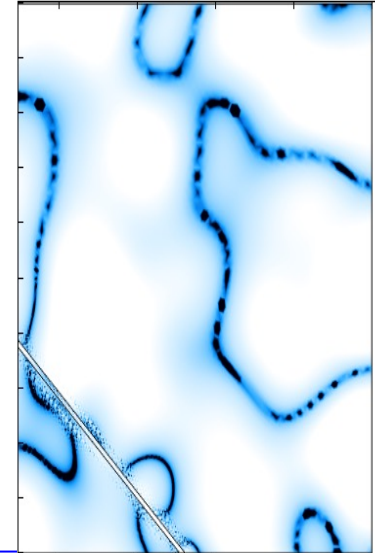


$t_s = \text{stage2.5}$



$t_s = \text{stage3}$

Repulsion



$t_s = \text{stage4}$

Slow Time

Conjectures :

Zero-polarity objects are not stable in isolated forms ;

string objects are always ended in boundaries and no-isolated string is observed.

The bubble are stable but in short living forms